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ABSTRACT

Is Economic Activity in the G7 Synchronized? Common Shocks versus Spillover Effects*

This Paper analyses the co-movement in activity, measured by GDP and industrial production, between the G7 countries for the period 1972-2002. For that purpose, a dynamic factor model is estimated using Kalman Filtering techniques. In addition to separating common and country-specific - idiosyncratic - developments of output, we try to identify the causes underlying the observed co-movement: to what extent is it driven by common shocks and to what extent can cross-country/cross-area spill-over effects account for the observed co-movement? We find that the output developments in G7 countries are driven to a substantial extent by common dynamics. A significant part of the co-movement, especially in the first half of the sample, can be explained by developments in the price of oil, an important and easily identifiable common shock. The analysis suggests that, in addition, area-specific common factors play an important role, separating the sample into a North American (US, Canada) and a continental European (France, Germany, Italy) area, with the UK and Japan being somewhat separate from these areas. We find that developments in the North American factor have a strong lagged impact on the continental European factor, while the reverse is not true. Furthermore, the strength of the cross-area spillovers from America to Europe appears to have become stronger over the sample period, suggesting that international linkages have increased in the process of globalization.

JEL Classification: E30 and F00

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1 Introduction

The issue of international business cycle linkages, or more generally, of possible co-movements in economic activity across countries and regions has recently resurfaced to the attention of analysts, policymakers and academic scholars. The simultaneous slowdown experienced to different degrees by all the G7 economies starting in the final part of 2000 underlines that the developments even in relatively large economies cannot always be analysed in isolation. For policymakers, the ability to gauge the nature and the magnitude of cross-country co-movements in economic activity may be crucial in order to assess the developments in their own domestic economy. This paper aims primarily at characterizing the common fluctuations amongst G7 economies by analysing the properties of real GDP growth in those countries. In particular, the paper first isolates and measures the historical evolution of the degree of output growth co-movements in the different countries and then assesses the relative importance of common shocks, affecting the different economies at the same time versus direct linkages between countries ("spillovers") in generating such co-movements. In addition, the analysis explores the role of oil price developments, which are considered a classical example of a common shock, in determining the joint fluctuation of real GDP growth in the G7 economies.

The methodology employed consists in the estimation of a dynamic common factor model for the G7 countries' GDP (and industrial production) growth using Kalman filtering techniques¹. The general model specification assumes the process for real GDP growth in each of the G7 countries to be driven by a country-specific autoregressive component and a latent component, which is common to all series. This latent component - or common factor - is also assumed to follow a univariate autoregressive process. In a subsequent step, "area-wide" common factors are introduced by allowing two separate univariate autoregressive common factors which are each shared by only a subset of countries. Finally, we try to disentangle "area-wide" common factors and "area-wide" spill-over effects by allowing the two "area-wide" common factors to interact. This is achieved by modelling the "area-wide" common factors as a multivariate autoregressive process, with each of the two common factors explaining its own and the other common factor's next period value.

The analysis shows that the G7 countries share common output dynamics with clearly identifiable common swings in activity across the G7. The paper ranks G7 countries according to two measures of synchronisation: the share of each country's total variance of real GDP growth explained by the variance of the common factor and, alternatively, the correlation between the common factor and the real GDP growth series. Furthermore, the paper finds statistical support for a (time-varying)

¹Modelling common fluctuation in economic variables by using the dynamic factor approach presents clear advantage as compared to simpler and more direct approaches like the one that analyses the evolution of pure bi-variate correlation (see among the others Baxter and Stockman (1989), Gerlach (1988), Stockman (1988) and more recently Doyle and Faust (2002). First, the analysis of simple correlation cannot allow for the separation of the idiosyncratic component from the purely common source of joint co-movements. Second, static correlation analysis, by definition, misses the possible persistence of common fluctuations.

effect of oil price developments on the common factor, confirming that oil prices, indeed, constitute one important variable partly responsible for the observed co-movement among economic activity in different countries. More concretely, while oil price developments are important in explaining the common factor during the 1970s, their relevance decreases in the last two decades. However, during the most recent downturn the role of oil prices appears to have played a somewhat more important role again.

Using the general model specification with one global common factor, the paper tries to disentangle common shocks from spill-over effects by exploiting the feature of the Kalman filter that it distributes the overall variance between the idiosyncratic and the common part of the system shocks. As a consequence, an initially idiosyncratic shock, which gets transmitted to other countries, will be identified as a common factor shock by the filter. From the analysis of the evolution of the variance of the idiosyncratic and the common factor disturbances, it appears that spill-over effects have gained in importance in explaining the co-movements among G7 countries' growth developments, especially from the mid-1980s to the mid-1990s.

The "area-wide" specification of common factors identifies significant "area-wide" common effects on real GDP growth developments in the G7 countries, with the "areas" being a North-American one (comprising the United States and Canada) and a Continental-European one (comprising Germany, France and Italy). Japan and the UK appear to be somewhat separated from these areas. The analysis with cross-area linkages indicates strong spill-over effects from the North-American area affecting the European area. At the same time, spill-over effects in the opposite direction - from Europe to North America - prove to be small and statistically insignificant. Interestingly, the model specification with inter-related "area-wide" common factors results in the loss of significance of the global common factor. This suggests that what was originally modelled as a pure global common factor was instead to a large extent capturing the mixture of joint fluctuations in a subset of countries' real GDP growth and cross-area spillover effects.

Within the family of the dynamic factor models there currently exist two main approaches: the linear state space model and the generalised dynamic factor (GDF) model.. The former approach, which this paper adopts, uses a parametric specification of the underlying dynamics, thereby allowing precise statistical inference. Unlike the present paper, none of the existing studies based on the linear state space model approach attempts to disentangle the possible underlying causes of the measured common dynamics. For example, Gregory, Head and Raynauld (1997) use dynamic factor analysis similar to that developed in this paper to study fluctuations in GDP, consumption and investment in the G7 countries for the period 1970 to 1993. The authors find significant world and country-specific components for all countries without any clear lead or lag relationship between the world component and individual country series. In a related paper, Gregory and Head (1999) analyse common factors in the behavior of productivity, investment and the current account for the G7 countries, with the main objective of assessing the validity of the intertemporal approach to the current account. The authors find that productivity and investment are strongly affected by a common world component, which in turn

is very similar to US movements in investment².

The rest of the paper is organised as follows: Section 2 sets the general model employed in the paper to estimate the common factor and briefly describes the dataset to which the model is applied. Section 3 contains the analysis of the model specification for the case of one common factor. In this section some evidence on the role of oil prices in determining the developments in the common factor is also presented. Section 4 presents the analysis involving "area-wide" common factors, while Section 5 introduces interdependencies between the "area-wide" common factors in order to identify possible cross-area spill-over effects. Section 6 concludes.

2 The linear state space model

The general idea underlying dynamic factor models is that the cross correlations between the components of a n -dimensional stochastic process Y_t can be captured by k unobservable factors $Z_{1,t}, \dots, Z_{k,t}$, where k is considerably smaller than n . As a special case, the dynamic factor model can be formulated as a linear state space model by assuming that Y_t depends linearly on the matrix of factors Z_t , which in turn follows a autoregressive process.

In this paper the general model specification assumes that the process for a n -dimensional stochastic process Y_t can be separated into three components:

$$Y_t = AY_{t-1} + BZ_t + \varepsilon_t \quad (1)$$

$$V[\varepsilon] = \begin{bmatrix} \sigma_1^2 & & 0 \\ & \ddots & \\ 0 & & \sigma_n^2 \end{bmatrix}$$

where σ_i^2 denotes $V[\varepsilon_i]$.

The B matrix measures the instantaneous impact (factor loadings or sensitivities) of the common factors on each series Y_i .

A is assumed to be diagonal in most specifications, thus capturing the core notion of the dynamic factor model that the co-movements of the multiple time series arise from the single source Z .

Furthermore, the dynamic process of the state vector Z_t is assumed to follow:

$$Z_t = DZ_{t-1} + \eta_t \quad (2)$$

The dynamics of the unobservable factors is univariate as long as D is diagonal. Moreover, an identification constraint is imposed on the variance-covariance matrix

²In a more recent paper, Kose et al. (2002) employ a Bayesian dynamic factor model to estimate common components in the main macroeconomic aggregates in a sixty-country sample covering seven regions of the world. They find significant evidence of an important effect of the world common factor and of less important regional factor.

of the disturbances η :

$$V[\eta] = Id(r)$$

With reference to the general notation introduced in equation 1 the actual general model implemented in the paper results in:

$$\mu_t = AY_{t-1}, B_t = B, \nu_t = 0, D_t = D, R_t = V[\varepsilon], Q_t = Id(r)$$

Given the relatively large dimension of the vector of estimated parameters θ we use a two-step procedure when computing ML functions, involving first the application of the Expectations Maximisation (EM) algorithm and subsequently the application of the BFGS maximisation algorithm provided by GAUSS.

2.1 Data

We use (seasonally adjusted) quarterly real GDP figures for the G7 countries from 1970.2 to 2002.2. In general, the series are taken from the International Monetary Fund database³. In subsection 5.1, (seasonally adjusted) monthly industrial production series of the G7 countries are considered. These data are taken from the IMF database, covering the period 1970.M2-2002.M2 at monthly frequency. All data series are log-differenced, demeaned and standardised.

Table 2.1 contains the cross-correlation coefficients for the GDP growth rates of the G7 countries. All the correlation coefficients are positive, with the highest correlation in the case of the USA-Canada and the France-Italy GDP growth rate pairs. With regard to the first order autocorrelation (see Table 2.2), all GDP growth rates except those for Germany exhibit positive autocorrelation, with Italy having the largest autocorrelation, followed by Canada and France.

Table 2.1 Cross-correlations among real GDP growth rates

	U.S.A.	Japan	U.K.	Canada	Germany	France	Italy
U.S.A.	1						
Japan	0.223	1					
U.K.	0.260	0.292	1				
Canada	0.529	0.193	0.200	1			
Germany	0.122	0.122	0.349	0.012	1		
France	0.248	0.205	0.246	0.223	0.398	1	
Italy	0.176	0.104	0.116	0.206	0.293	0.531	1

Table 2.2 First order autocorrelations among real GDP growth rates.

	U.S.A.	Japan	U.K.	Canada	Germany	France	Italy
$corr(X_t, X_{t-1})$	0.279	0.097	0.057	0.374	-0.087	0.310	0.449

³However, in the case of Japanese GDP data the OECD database was used, as the IMF series exhibits a spike in 1980.1, reflecting a change in statistical methodology for calculating Japanese GDP. In addition, the IMF series is not seasonally adjusted prior to that date.

3 The case of one common factor

This first application of the general model depicted in Section 2 involves a single common factor Z . We can then rewrite Eq.(1) and (2) as:

$$\begin{aligned} Y_{i,t} &= a_i Y_{i,t-1} + b_i Z_t + \varepsilon_{i,t} \\ Z_t &= d Z_{t-1} + \eta_t \end{aligned} \tag{3}$$

In this case, since the $\varepsilon_{i,t}$ are serially and contemporaneously uncorrelated, co-movements among the $Y_{i,t}$ are explained only by the single common factor.

(Insert Figure 1 here)

Figure 1 plots the estimated common factor. According to this factor the G7 economies experienced four major downturns since 1970: In the mid-1970s, early 1980s and early 1990s, and most recently in 2000. The downturns in the mid-1970s and early 1980s were both very sharp, while the downturn in the early 1990s was preceded by a generally delining trend starting in the second half of the 1980s. Similarly with respect to the upturns, some were very sharp (1974-1975, 1993) while the downturn in the early 1980s was followed by long period of gradual expansion. These activity patterns and their timing conform reasonably well with common wisdom on global economic developments over recent decades. In particular, the first and second downturns correspond to the timing of the two oil price shocks, although the impact of the latter on economic activity appears to be much less pronounced.

The parameter estimates are given in Table 3.1. The lagged dependent variable is significant only in the case of Canada, Germany and Italy, while the impact coefficients of the global component on the GDPs (b_i) are all significant and similar in magnitude across the different countries. The global factor exhibits a relatively high degree of autocorrelation, as indicated by the value of almost 0.7 for the coefficient d , which suggests high persistence of common output developments on real GDP growth in each of the G7 economies.

Table 3.1 Parameter estimates (Model with one common factor)

	U.S.A.	Japan	U.K.	Canada	Germany	France	Italy
a_i	0.115 (0.086)	-0.055 (0.087)	-0.097 (0.088)	0.248 (0.084)	-0.277 (0.086)	0.001 (0.094)	0.284 (0.084)
b_i	0.299 (0.075)	0.309 (0.077)	0.331 (0.078)	0.238 (0.071)	0.408 (0.081)	0.496 (0.088)	0.336 (0.074)
σ_i	0.881 (0.058)	0.910 (0.060)	0.898 (0.060)	0.875 (0.057)	0.839 (0.060)	0.721 (0.064)	0.778 (0.054)
d	0.693 (0.087)						

$$Y_{i,t} = a_i Y_{i,t-1} + b_i Z_t + \varepsilon_{i,t}$$

$$Z_t = dZ_{t-1} + \eta_t$$

The estimation of model (3) as a simple univariate first order autoregressive process⁴ validates the inclusion into the model of a dynamic common factor⁵.

(Insert Figure 2 here)

Figure 2 plots the common factor - weighted by its country-specific impact coefficient b_i ⁶ - together with the actual GDP series for the US, Japan and Germany. It appears that the slowdown in the mid 1970s is indeed well-explained by the common factor⁷. Only in Japan did GDP growth in one quarter deviate significantly from the level suggested by the common factor. During no other downturn does the common factor appear to explain country-specific growth performance as well as in this first one, as growth rates in the various countries fluctuate more strongly around the path suggested by the common factor. Nonetheless the common factor appears to be able to explain some important general cyclical trends in GDP growth in the individual countries. In addition, it helps to identify a few episodes as more or less country specific. In the case of the US, the strong growth performance in 1983/1984 appears to be very much a country specific phenomenon, similar to the recession experienced in 1990/1991. In the case of Germany, the “post-reunification boom” from 1989 to 1991 stands out as a country-specific event. Regarding Japan, it is interesting to note that the slow growth performance in the 1990s - and, especially, in the second half of the decade - is largely a country-specific phenomenon, reflecting the delayed effects of the bursting of the asset price bubble in the early 1990s. Moreover, the difference in volatility between the common factor and the quarterly GDP growth

⁴It can be shown that the marginal dynamics of each $Y_{i,t}$ implied by the common factor model is an ARMA(2,1) process and thus allows for significantly more complex dynamics than the simple AR(1) in this reduced specification.

⁵The value of the AIC in the case of the simple AR(1) specification is -1249.8 compared to -1190.9 in the case of the dynamic common factor model.

⁶In Figure 2 the impact of the common factor on real GDP growth appears to be similar in the case of the US, Japan and Germany. However, the series actually differs by a factor given by the b_i s in Table 3.1.

⁷In subsection 3.2 the paper provides empirical evidence supporting the significant role of oil price developments in determining the evolution of the common factor.

figures increases substantially in the latter half of the 1990s. This may indicate that the policy measures intended to revive the Japanese economy have introduced a substantial amount of idiosyncratic volatility into the economy⁸.

Based on the model estimates, it is possible to derive some measures of synchronisation in the G7 economic developments, by looking both at the amount of volatility of each single real GDP growth series that is explained by the volatility of the common factor and to the impact effect of the evolution of the common factor on each of these series. Table 3.2, which reports the shares, S_i , of the total real GDP growth variance accounted for by the common factor, documents the particularly large role played by the common factor in the case of France and Italy, where its variance explains around one half to one third of these countries' real GDP growth variance. For the other countries the share is somewhat lower but still accounts for one sixth to one fourth of these countries' growth variations.

Table 3.2 Shares of variance of real GDP growth accounted for by the common factor.

	U.S.A.	Japan	U.K.	Canada	Germany	France	Italy
S_i	0.206	0.170	0.186	0.168	0.235	0.477	0.349

In addition, we compute the correlations between the global factor and the GDP series. Unlike in the case of the share of variance explained by the common factor, here the emphasis is more on the contemporaneous impact of the common factor on a country's GDP growth rate, rather than on the entire effect (including lagged responses to the common factor), which is captured by the b_i s in Table 3.1. Table 3.3 shows that this correlation is relatively high for all countries, especially for the continental European countries. In addition, with the exception of Canada (whose series is strongly correlated with the one of the U.S.A.), all series of the G7 countries have higher correlations with the global factor than with the series of any other countries (see Table 2.1 for reference). It is interesting to notice that the ranking of countries' degree of synchronisation emerging from Tables 3.2 and 3.3 is rather different from the ranking according the values of the b_i s in Table 3.1. The Continental-European block of the G7 countries remains the most affected by the common factor, but the US position is higher in the ranking by degree of synchronisation as it is in terms of total effect of the common factor. Japan appears to be the country whose real GDP growth is least synchronised with the common factor.

Table 3.3 Correlation of the GDP series with the global factor.

	U.S.A.	Japan	U.K.	Canada	Germany	France	Italy
$Corr(Z_t, Y_{i,t})$	0.517	0.463	0.485	0.476	0.542	0.781	0.640

Figure 3 shows the evolution of the correlation between Z_t and $Y_{i,t}$ over time for the G7 countries using a 4-year rolling window. It is apparent that the correlation of individual countries' growth rates with the common factor has overall been fairly

⁸Alternatively it may reflect shortcomings in the GDP statistics, although it seems difficult to explain why such statistical problems may have become more prevalent during the 1990s.

high (up to 0.7 in the early 70s), although a moderately declining trend can be identified. The only country, which saw a slight increase in the correlation, is France, while Canada's correlation trend was basically flat. On the other side, strong declines in the correlation trend can be observed especially for the US and Japan. Thus overall it appears that the synchronisation of business cycles has declined over the past three decades. Against that background, the most recent pick-up in correlation is particularly noteworthy, as it underlines the synchronised nature of the most recent downturn.

(Insert Figure 3 here)

3.1 The synchronisation of G7 real GDP growth: common shocks vs. spill-over effects.

Based on the correlation evidence alone it is, however, not possible to say anything about the reasons for this decline or, more generally, about the reason for the overall level of synchronisation of business cycles among the G7 countries. In principle, synchronisation can be attributed to three different causes: all countries are affected by a common shock, to which they react in similar ways. Second, a subgroup of the countries - possibly only a single country - experiences a shock, which is transmitted to the other countries through the various international transmission channels. And third, the countries happen to experience similar country-specific shocks. All these cases would be captured as a shock to the common factor in the current estimation framework, without being able to distinguish between the different cases.

Although a quantification of the different explanations to the observed level of overall synchronisation is not possible in the current framework, some insights into the causes behind changes in the degree of synchronisation documented above may be, nonetheless, possible. An increase in the variance of idiosyncratic shocks ε_{it} in the measurement equation, which one might consider a decrease in international synchronisation, would result in a decline of the correlation between a country's growth rates and the common factor, while leaving the covariance unchanged. In contrast, an increase in the variance of the common factor, as captured by an increase in the error term η_t in the transition equation, would be reflected in an increase of both the correlation and the covariance between the growth rate and the common factor⁹. Thus, an increase in the synchronisation of a country's growth performance with the international business cycle would be reflected in an increase in the correlation between the two series, either due to a decline in the idiosyncratic growth fluctuations or due to an increase in the variance of the common shock, whose impact on the correlation is more than offset by the associated increase in the covariance between the two series.

⁹This follows directly from the expression for the covariance between y_{it} and z_t :

$$Cov(Y_{i,t}, Z_t) = \frac{b_i}{(1-a_i b_i)(1-d^2)} \sigma_\eta^2$$

In addition, it is even possible to make inferences about the changing relative importance of common shocks and spillover effects. If merely the variance of η_t changes, this would indicate a change in the relevance of common shocks for international growth fluctuations. If, however, the change in the variance of η_t is accompanied by a change of the variance of ε_{it} in opposite direction this would indicate a change in the importance of spillover effects. The case of strengthening international transmission channels may help to illustrate this case. Let us assume for the sake of argument that initially there are no common shocks and no spillover effects. In that case the growth of the various countries would not be correlated except as the result of sampling errors. If due to increasing global integration the fluctuations in a certain country start to affect other countries in a systematic (and linear) way, this introduces a certain degree of comovement into the system, which in our modeling framework would be picked up by the common factor. Concretely, the part of the idiosyncratic shock which causes spillover effects, will no longer be counted as a idiosyncratic shock but will instead be categorized as a common shock. As a consequence, the variance of the idiosyncratic shock in the country from which the spillover effects originate will decrease, while the variance of the common shock will increase. In principle, therefore, even the countries from which the spillovers originate could be identified. Of course, such a clear pattern would apply only in the theoretical *ceteris paribus* case. In reality other factors may play a role as well and may dominate the development of the two variances. For example, an increase in international spillovers may be masked by an autonomous increase in idiosyncratic volatility or a simultaneous decline in the variability of common shocks. Nonetheless, it is useful to take a close look at the evolution of the variance of the two shocks over time.

(Insert Figure 4 here)

Figure 4 depicts the evolution of the variance of η_t and ε_{it} using again a 4-year rolling window. The variance of η_t declines more or less continuously until the mid-1980s. After that, it remains relatively constant, with a moderate gradual increase up to the mid-1990s, followed by a relatively sharp drop in 1997. In 2001, this drop is partly reversed again. Regarding the variance of the ε_{it} , no uniform pattern exists. For a number of countries, the variance of ε_{it} has seen a noticeable decline in the second half of the sample similar to the variance of η_t . This is particularly the case for the US, Canada, the UK and Italy. Unlike the other countries, Japan experienced a marked increase in the variance of ε_{it} in the second half of the 1990s. The timing of the increase in Q2 1997 suggests that it might be related to the fiscal tightening implemented at that time.

It seems reasonable to assume that the decline in the variance of η_t , and thus of Z_t , over the first half of the sample period was the result of the declining importance of oil price disturbances and therefore of truly common shocks, rather than the result of declining global integration and reduced spill-over effects. As this effect has dominated this period it would be difficult to identify more gradual shifts due, for example, to increasing international spill-over effects. The decline in the

variance of ε_{it} observed for a number of countries over the same period may be the result of lower idiosyncratic policy volatility related to the consequences of the oil price shocks to which countries reacted in very different ways. The results do unfortunately not provide any clear evidence as to whether international spill-over effects have become more important over the sample period, as there is very little evidence of a general decline in idiosyncratic volatility associated with increased common volatility. However, for some subperiods such a pattern can be identified for individual countries.

The strong increase of the variance of the Japanese idiosyncratic shock in Q2 1997 is particularly striking, as it is accompanied by a noticeable contemporaneous decline of the variance of the common shock. This movement in both series is partly reversed in Q3 2001. Although this finding would be consistent with a temporary isolation of Japan from the other G7 countries, in the sense that spill-overs from shocks to the Japanese economy were reduced during that period, it appears difficult to explain why such a sudden and temporary disconnect should have occurred. A possible explanation might be that the increase in the consumption tax in Japan in early 1997, which contributed to a slowdown in economic activity, marked the beginning of a period of domestic policy volatility characterised by limited international ramifications.

Possibly more interestingly, if one focuses on the average idiosyncratic shock variance for all countries, the gradual increase in the variance of the common shock from the mid-1980s until the mid-1990s coincides with a declining trend in the idiosyncratic shock variance. Thus, during this decade the effects of increasing international integration may indeed have dominated the evolution of the error variances. Of course, this finding is merely suggestive of such an interpretation, as the same pattern could be the result of two completely independent developments in the two variance series. However, as the pattern can be observed for a relatively extended period of time, it seems to be driven by a gradual process, such as globalisation, rather than a one-time event, such as a change in the policy framework.

3.2 The common factor and oil prices

To the extent that the observed comovement in G7 activity is driven by common shocks rather than spillover effects, fluctuations in oil prices may be one specific and easily identifiable underlying factor driving the common factor. This is, for example, suggested by the coincidence of the first two G7 recessions identified by the common factor with the two oil price shocks in the early and late 1970s. In order to test for the role of oil prices more formally, we regressed the common factor on various lags of the log changes of the oil price¹⁰, refining the specification from general to specific. The low values of the Durbin-Watson coefficient indicate a substantial

¹⁰We used the price of Western Texas oil. The original price quotation in US-dollars was converted into a weighted currency price taking exchange rate movements among the currencies of the G7 countries into account.

degree of autocorrelation in the error term, which we take explicitly into account in the estimation. Table 3.4 contains the estimation results.

Table 3.4 Regression of Z on log differenced oil prices (1970.2 to 2002.2)

α_1	α_3	α_4	α_5	AR_ϵ
-0.015	-0.035	-0.028	-0.019	0.806
(0.009)	(0.010)	(0.010)	(0.010)	(0.054)
R^2				
0.70				
$Z_{1,t} = \alpha_1 oil_{t-1} + \alpha_3 oil_{t-3} + \alpha_4 oil_{t-4} + \alpha_5 oil_{t-5} + \epsilon_t$				

In general, the high autocorrelation in the error terms indicates that oil prices by themselves are not able to explain the persistence in the common factor and that therefore other factors are likely to play an important role in explaining the movement of the common factor. Nonetheless oil prices appear to be an important part of the explanation for the comovement of the G7 economies. Figure 5 depicts the actual common factor and the estimated values (excluding the autoregressive error component) obtained in the oil regression. In line with perceived wisdom, oil prices were particularly important during the two recessions in the mid-1970s and the early 1980s, although the renewed slowdown around 1980-1981 seems to have been relatively unrelated to oil prices. Likewise the G7 recession in the early 1990s appears to be due largely to other factors than oil prices. In contrast, during the latest downturn in 2000-2001 oil prices again seem to play a non-negligible role. In general, it appears that during the second half of the sample period a phase shift has occurred, with output reacting more slowly to changes in oil prices.

(Insert Figure 5 here)

Thus, a uniform lag structure over the entire sample may not be appropriate and we reestimated the model for two separate subperiods: from 1970:2 to 1986:1 and from 1986:2 to 2002:2. Figures 6 and 7 show the respective estimated common factors. The estimation for the first subsample (see Table 3.5) shows that oil prices become even more important for the first two recessions when one allows for a change in the structural relationship. Similarly, although clearly less important in the second half of the sample period oil prices maintain some explanatory even in the later subperiod (see Table 3.6), which was characterised by much less pronounced swings in oil prices. The different lag structure in the two sub-samples also underlines the changed response of economic activity to oil price shocks, with the response in the first sub-period being considerably more immediate than in the second.

(Insert Figure 6 and 7 here)

Table 3.5 Regression of Z_1 on log differenced oil prices (1970.2 to 1986.1)

α_3	α_4	AR_ε
-0.074	-0.060	0.817
(0.016)	(0.016)	(0.075)
R^2	DW	
0.78	1.62	

$$Z_{1,t} = \alpha_3 oil_{t-3} + \alpha_4 oil_{t-4} + \varepsilon_t$$

Table 3.6 Regression of Z_1 on $(oil_t, \dots, oil_{t-5})$ from 1986.2 to 2002.2

α_5	α_7	α_9	α_{10}	AR_ε
-0.019	-0.021	-0.020	-0.020	0.817
(1.075)	(1.075)	(0.016)	(0.016)	(0.075)
R^2	DW			
0.71	1.52			

$$Z_{1,t} = \alpha_5 oil_{t-5} + \alpha_7 oil_{t-7} + \alpha_9 oil_{t-9} + \alpha_{10} oil_{t-10} + \varepsilon_t$$

Overall, these results suggest that a substantial part of the common fluctuations in G7 activity may be explained by oil shocks. The current estimates provide a lower bound for the importance these shocks, as there may exist important other factors influencing economic activity across countries. In general, they can, however, be expected to be quantitatively less important individually and possibly more difficult to measure. Therefore, the dynamic factor model may be a convenient tool to capture their overall effect without having to specify all factors separately. The costs involved in such a strategy is that one captures in addition to comovement introduced by common shocks also comovement resulting from spill-over effects between countries¹¹.

4 "Areas" Model

In this section, the general model is extended by introducing dynamic factors which are common only to a sub-set of series, in addition to a single factor common to all the G7 real GDP growth series¹². More precisely, let us consider n areas, and for

¹¹In this respect is important to note, however, that even if all common shocks were properly measured and introduced into the estimation procedure it would be very difficult to disentangle the direct effect of these shocks on a country's growth rate and the indirect effects from spill-overs of the common shock on other countries.

¹²The estimation of the general model (1) with two common factors shared by all countries (not reported here) suggests that rather than being influenced only by one global factor, subsets of countries may be affected by area-specific common factors. When adding a second global factor to the one factor model of Section 3, one of the global factors resembles very closely the original common factor. The second factor appears to capture asymmetries among the countries, as the factor loadings are positive for some countries and negative for others. In particular, we find that the factor loadings for the US and Canada share the same sign, while the factor loadings for the Continental European countries France, Germany and Italy have the opposite sign. The factor loadings for the second factor in the case of Japan and the UK are insignificant.

each area (area i) k_i series. We will refer to these series by using the notation: $Y_{i,t}^j$, where $j = 1, \dots, k_i$ indexes the series of the i^{th} considered area.

Let W_t be an unobserved factor affecting all of the series, and $N_{i,t}$ be a factor common to all the series in area i . We will refer to them as the global common and area-specific common factors. Each series $Y_{i,t}^j$ can thus be decomposed into four separate components:

$$Y_{i,t}^j = a_i^j Y_{i,t-1}^j + b_i^j W_t + c_i^j N_{i,t} + \varepsilon_{i,t}^j \quad \forall i \quad \forall j \quad (4)$$

Here, b_i^j measures the impact of W_t on the j^{th} series of area i and c_i^j measures the impact of the area-specific common component on the j^{th} series of area i . As before, we assume that $(\varepsilon_{1,t}, \dots, \varepsilon_{n,t}, W_t, N_{i,t})$ are uncorrelated at all lead and lags, which is achieved by assuming that ε is a white noise and that ε, W and the N_i s are independent.

Denoting with $(\sigma_i^j)^2$ the variance of $\varepsilon_{i,t}^j$, we have

$$V[\varepsilon] = \begin{bmatrix} \begin{bmatrix} (\sigma_1^1)^2 & & 0 \\ & \ddots & \\ 0 & & (\sigma_1^{k_1})^2 \end{bmatrix} & \dots & 0 \\ & \vdots & \vdots \\ & 0 & \dots & \begin{bmatrix} (\sigma_n^1)^2 & & 0 \\ & \ddots & \\ 0 & & (\sigma_n^{k_n})^2 \end{bmatrix} \end{bmatrix}$$

Both, the global and the area-specific common factors are assumed to follow univariate autoregressive processes of order one:

$$W_t = d_w W_{t-1} + \eta_{w,t}$$

$$N_{i,t} = d_i N_{i,t-1} + \eta_{i,t} \quad (5)$$

where we add the following identification condition:

$$V \begin{bmatrix} \eta_{w,t} \\ \eta_{1,t} \\ \vdots \\ \eta_{n,t} \end{bmatrix} = Id_{n+1}$$

The results of the two-factor model suggest that two distinctive area factors may play a role: a North-American (US and Canada) and a Continental European (France, Germany and Italy) one. As the loading coefficients for Japan and the UK were insignificant it is not clear whether or where these countries should be included. Based on the results from various area specifications, we chose to exclude

Japan from the analysis, as it does not appear to belong to any of the areas. For the UK, we estimated the model separately for the two cases of the UK belonging to the North-American and the Continental-European area. Using the notations introduced in 4, $i \in \{1, 2\}$ indexes the area, and $j \in \{I, II, III, IV\}$ indexes the j^{th} country in the considered area.

Figure 8 plots the three common factors estimated. The global factor W_t shares the main feature of the global factor obtained earlier in the case of a single common factor for all countries. Thus although in the present specification area-specific developments are taken into account, the six analysed countries still clearly show a high degree of comovement - even across areas and the common dynamics are more persistent than in the single-factor model as indicated by the autoregressive coefficient of the transition equation. In addition to the globally shared dynamics the estimation results also show that area-specific common dynamics play an important role. Although the two area factors show some similarities in their evolution, they capture important differences in the two areas. In this respect, more pronounced downturns in activity in the North-American (+UK) factor than in the Continental-European factor in the early 1980s can be seen. Furthermore, the effect of the German reunification boom and subsequent decline in activity, which clearly affected neighboring countries as well and thus shows up as common movement of these countries, can be identified in the Continental-European factor, while being absent from the North-American (+UK) factor. As shown in Table 4.1 the persistence of the global factor is considerably higher than that of the two area-specific factors, whose autoregressive coefficients are very similar. For most countries, the area-specific factor is much more important than the truly global factor in explaining growth developments (see Table 4.2) Only in the case of the UK and France does the share of variance explained by the global factor exceed that explained by the respective area factors, with the important difference that both factors together explain only a small share of growth variance in the case of the UK (15%), while in the case of France the two factors play a much more important role (65% explained by the two factors).

(Insert Figure 8 here)

Table 4.1 Parameter estimates (Model with global and two area factors)
 UK included in the North-American area

	U.S.A.	U.K.	Canada	Germany	France	Italy
a_i^j	-0.263 (0.165)	-0.203 (0.120)	0.198 (0.080)	-0.284 (0.084)	0.073 (0.107)	0.224 (0.083)
b_i^j	0.497 (0.151)	0.433 (0.141)	0.255 (0.085)	0.236 (0.084)	0.318 (0.096)	0.204 (0.078)
c_i^j	0.752 (0.281)	0.108 (0.176)	0.363 (0.125)	0.390 (0.100)	0.561 (0.124)	0.378 (0.093)
σ_i^j	0.213 (0.889)	0.808 (0.110)	0.742 (0.058)	0.828 (0.062)	0.605 (0.010)	0.740 (0.058)
d_w	0.726 (0.100)	d_1	0.288 (0.178)	d_2	0.553 (0.136)	

$$Y_{i,t}^j = a_i^j Y_{i,t-1}^j + b_i^j W_t + c_i^j N_{i,t} + \varepsilon_{i,t}^j \quad \forall i \quad \forall j$$

$$W_t = d_w W_{t-1} + \eta_{w,t}$$

$$N_{i,t} = d_i N_{i,t-1} + \eta_{i,t}$$

Table 4.2 Shares of variance accounted for by common factors

	USA	UK	Canada	Germany	France	Italy
S_w	0.381	0.307	0.194	0.083	0.197	0.131
S_i	0.570	0.018	0.170	0.173	0.428	0.283

S_w : share of variance accounted for by the global factor

S_i : share of variance accounted for by the area-specific factor

The small share of the growth variance explained by the area factor in the case of the UK may indicate that it is more appropriately modeled as belonging to the Continental-European factor. Figure 9 and Tables 4.3 and 4.4 report the results of this alternative specification. Overall, it appears that the main features of the area factors and the global factor prove to be relatively robust to this modification. However, also in this specification UK output growth does not appear to be strongly affected by the area specific factor, with the share of variance explained by the area factor actually being slightly lower than in the alternative specification. In contrast to the previous results, however, the global factor explains now almost one fourth of the UK output variance. The two specifications can also be compared more formally: Since the number of unknown parameters is the same in the two specifications, using the Akaike criteria to compare the two models amounts to comparing the two log-likelihoods of the models. According to this test the specification with the UK part of the North-American area performs slightly better than the alternative.¹³ A separate estimation of the models two sub-samples of roughly equal length (1970.2-1986.2 and 1986.3-2001.4) suggests that this slightly better fit mainly reflects the growth dynamics of the first sub-sample, as the log likelihoods in the second sub-sample are basically identically, suggesting that the UK could equally well be seen as belonging

¹³The log likelihood of the model with the UK in the North-American area is -974.518 , while that for the alternative model with the UK part of the Continental-European area is -975.141 .

to North-American or the Continental-European area.¹⁴ In any case, the share of variance explained by the area factor in the case of the UK is small and the concrete specification choice does not appear to affect the qualitative results of the analysis.

(Insert Figure 9 here)

Table 4.3 Parameter estimates (Model with global and two area factors)

UK included in the Continental-European area

	U.S.A.	Canada	U.K.	Germany	France	Italy
a_i^j	-0.288 (0.171)	0.185 (0.080)	-0.166 (0.108)	-0.291 (0.085)	-0.044 (0.101)	0.229 (0.083)
b_i^j	0.444 (0.141)	0.251 (0.095)	0.350 (0.123)	0.181 (0.101)	0.289 (0.123)	0.183 (0.097)
c_i^j	0.816 (0.267)	0.345 (0.140)	0.098 (0.142)	0.456 (0.108)	0.557 (0.123)	0.395 (0.098)
σ_i^j	0.015 (0.307)	0.778 (0.067)	0.859 (0.077)	0.811 (0.066)	0.625 (0.088)	0.737 (0.058)
d_w	0.759 (0.098)	d_1	0.333 (0.237)	d_2	0.534 (0.146)	

$$Y_{i,t}^j = a_i^j Y_{i,t-1}^j + b_i^j W_t + c_i^j N_{i,t} + \varepsilon_{i,t}^j \quad \forall i \quad \forall j$$

$$W_t = d_w W_{t-1} + \eta_{w,t}$$

$$N_{i,t} = d_i N_{i,t-1} + \eta_{i,t}$$

Table 4.4 Shares of variance accounted for by common factors

	USA	Canada	UK	Germany	France	Italy
S_w	0.327	0.207	0.231	0.054	0.183	0.121
S_i	0.672	0.159	0.012	0.231	0.421	0.298

S_w : share of variance accounted for by the global factor

S_i : share of variance accounted for by the area-specific factor

5 Spill-over effects

As the above analysis shows, the growth performance in the individual G7 countries contains a common element, which can be described by autoregressive common factors - either global or area-specific. In addition to being able to describe the common component, it would be useful to gain a better understanding of the determinants of the co-movement of growth rates. As shown above, common shocks in the form of oil price movements can explain some part of the observed co-movement. In this section, the issue of spill-over effects will be addressed in more detail: To what extent do developments in one country/area affect growth in other countries/areas?

¹⁴For the sub-period 1970.2-1986.2 the likelihood for the model with the UK in the North-American area is -487.178 , compared to -488.455 in the case of the alternative specification.

Unfortunately, such exercise is complicated by the fact that without clear a priori identifying restrictions, contemporaneous spill-overs, i.e. spill-overs which affect another country within the same period, can not be analysed. Thus we have to rely on the intertemporal pattern of impulse and response to measure spill-over effects. Such a procedure will, of course, only allow insights if a substantial part of cross-country spill-over effects operate relatively slowly, taking, for example, in the present case up to one quarter to materialise.

We tried to identify cross-country spill-over effects through appropriate adjustments of the model specification. In particular, two approaches were initially chosen. First, the A matrix, instead of being diagonal, was specified as a non-diagonal matrix. In this case, the model becomes a mixture of a first-order VAR and a dynamic factor model, where common movements in the variables can be driven by the common factor and through cross-country spill-over effects, captured by the off-diagonal elements of the A matrix. Second, instead of affecting other countries directly through the A matrix, growth developments in the individual countries were specified as affecting each other through its impact on the common factor. To that end, lagged growth rates of each country were added to the transition equation. In this case, growth in each country is thus influenced by an index of lagged growth rates in the different countries. Unfortunately, the estimation results using these specifications were not very encouraging. In particular, many of the coefficients capturing the spill-over effects turn out to be insignificant and/or have the "wrong" sign. As one reason for these findings may be the large number of parameters to be estimated, especially in the case of the first specification using a non-diagonal A matrix, we chose an alternative specification, in which spill-over effects exist between areas rather than countries. More specifically, we model spill-over effects by allowing the D matrix to be non-diagonal, thereby creating lagged links between the area-specific common factors. Initially, we estimated the model with a global factor and two area factors connected through spill-over effects. The results showed that the global factor changes dramatically in this case and no longer lends itself to an easy economic interpretation. Furthermore, we find that dropping the global factor from the model does not affect the results of the analysis and leaves the Akaike criterion basically unchanged.¹⁵ Thus we report here only the results for the model without the global factor.

Concretely, the measurement equations are:

$$Y_{i,t}^j = a_i^j Y_{i,t-1}^j + c_i^j N_{i,t} + \varepsilon_{i,t}^j \quad \forall i \quad \forall j$$

and the transition equations are:

$$\begin{bmatrix} N_{1,t} \\ \vdots \\ N_{n,t} \end{bmatrix} = \begin{bmatrix} d_{1,1} & \cdots & d_{1,n} \\ \vdots & \ddots & \vdots \\ d_{n,1} & \cdots & d_{n,n} \end{bmatrix} \begin{bmatrix} N_{1,t-1} \\ \vdots \\ N_{n,t-1} \end{bmatrix} + \begin{bmatrix} \eta_{1,t} \\ \vdots \\ \eta_{n,t} \end{bmatrix}$$

¹⁵In fact, the Akaike criterion is slightly higher for the model with the global common factor included for the specification with the UK belonging to the North-American area, it while it is slightly lower in the alternative specification with the UK in the Continental-European area. In any case, the differences are very small.

where $V[\eta_t] = Id_n$. The state vector N_t is thus assumed to follow a VAR process of order one.

Given the slightly higher value of the Akaike criterion, we report the results for the specification with the UK being part of the North-American area. Figure 10 shows that the area-specific factors are very similar to the ones in specification with global factor and either independent or related area-specific common factors. The Akaike criterion suggests that the present specification is in fact superior to the model with the global factor and two independent area-specific factors, despite the fact that it contains fewer factors to explain the shared growth dynamics.

Regarding the interaction between the two area-specific common factors it is interesting to note that the North-American factor has a strong lagged impact on the Continental-European factor (in Table 5.1 $d_{2,1}$ is large and statistically significant), while the reverse is not true; the coefficient for the lagged Continental-European factor, $d_{1,2}$, in the equation describing the evolution of the North-American factor is small and insignificant. This finding is also illustrated by the impulse response functions in Figure 11, where the impact of an innovation in the area-specific factors on the various countries is depicted.

Table 5.1 Parameter estimates (Model with two interrelated area-specific factors)
UK included in North-American area

	U.S.A.	Canada	U.K.		Germany	France	Italy
a_i^j	-0.173 (0.109)	0.117 (0.090)	-0.047 (0.087)		-0.277 (0.084)	0.008 (0.098)	0.194 (0.086)
c_i^j	0.661 (0.119)	0.494 (0.123)	0.297 (0.101)		0.432 (0.126)	0.546 (0.100)	0.455 (0.061)
σ_i^j	0.621 (0.100)	0.715 (0.064)	0.926 (0.061)		0.826 (0.062)	0.666 (0.075)	0.693 (0.061)
$d_{1,1}$	0.629 (0.119)	$d_{1,2}$	0.018 (0.101)	$d_{2,1}$	0.395 (0.123)	$d_{2,2}$	0.434 (0.126)

$$Y_{i,t}^j = a_i^j Y_{i,t-1}^j + c_i^j N_{i,t} + \varepsilon_{i,t}^j \quad \forall i \quad \forall j$$

$$N_t = (d_{i,j}) N_{t-1} + \eta_t \quad i \in \{1, 2\}, j \in \{1, 2\}$$

(Insert Figures 10 here)

(Insert Figures 11 here)

The area-specific shocks explain roughly half of the growth variance in the case of the US and Canada, with virtually all the explanatory power coming from innovations in the North-American factor (see Table 5.2). In the case of the UK, the overall share explained by the factors is again considerably lower, but also comes virtually exclusively from the North-American factor. For the Continental-European countries also most of the variance is explained by their "own" area-specific factor. However, for these countries the "other" area-specific factor also accounts for a substantial share of the growth variance. In relative terms, the contribution is around

one third (Germany) to one half (Italy) of the Continental-European factor. Overall, Germany and the UK are the countries with the smallest share of the growth variance explained by the common factors.

Table 5.2 Shares of variance accounted for by the innovations of the common factors

	USA	Canada	UK	Germany	France	Italy
S_1	0.604	0.482	0.140	0.071	0.175	0.172
S_2	0.000	0.000	0.000	0.195	0.376	0.321

S_i : share of variance accounted for by the innovations of area-specific factor N_i

Using the estimation results, it is possible to calculate hypothetical area-specific factors, which show the evolution of the factors assuming that the respective areas had not been affected by developments in the other area. For the North-American factor the two series, with and without the effect of the Continental-European factor, are, as expected, virtually identical and therefore omitted. For the Continental-European factor some interesting difference can, however, be identified (see Figure 12). For example, it appears that in the early 1970s Europe's growth performance was lifted up by the positive spill-over effects from North America. In contrast, the slowdowns in the early 1980s would have been less pronounced, if Europe had been shielded from the influence of developments in North America. Likewise in the early 1990s European growth was strongly negatively affected by the recession in the US and also the most recent downturn in Europe was to a considerable part a reflection of adverse developments in North America. At the same time, however, the subsequent growth reversal in North America has also helped to revive European growth, bringing the Continental European factor back to a level where it would have been without the intermittent downward pressure from the North-American factor.

(Insert Figure 12 here)

When the UK is included in the Continental-European area the results are very similar. This can, for example, be seen in the shares of variance explained by the two area-specific factors (see Table 5.3). In the case of the US and Canada, the share of variance explained by both the North-American and the European factor increases slightly, but the effect of the European factor on the North-American factor remains small and insignificant¹⁶. In the case of the European countries, the share of variance explained by the Continental-European factor decreases slightly for Italy, while it increases for France and Germany. The effect of the North-American factor on the European one is reduced in this specification, except in the case of Germany, suggesting that possibly part of the spill-overs in the previous specification originated in the UK. For the UK itself the overall share of variance explained by the two factors remains virtually unchanged, although, of course the bulk of the explanation now comes from the "own" - European - factor.

¹⁶The estimated value of the parameter $d_{1,2}$ (see Table 7.1) in the specification with the UK in the Continental European factor is 0.079 and its standard deviation is 0.100.

Table 5.3 Shares of variance accounted for by the innovations of the common factors

	USA	Canada	UK	Germany	France	Italy
S_1	0.632	0.485	0.038	0.070	0.156	0.139
S_2	0.007	0.006	0.102	0.224	0.392	0.301

S_i : share of variance accounted for by the innovations of area-specific factor N_i

5.1 Industrial production

A similar picture arises if one uses industrial production data instead of GDP¹⁷. The advantage of industrial production figures is that they are available at a monthly frequency. Thus it might be possible to better identify spill-over effects to the extent that these materialise relatively quickly. On the other hand, industrial production data tend to be more volatile than GDP figures and it may therefore be more difficult to extract systematic relationships from them. The results, however, show that some meaningful relationships and co-movements also exist for industrial production. In fact, the global common factor for industrial production is very similar to the factor for GDP, with a correlation coefficient (using a 7 year rolling window) of between 0.5 and 0.9 between the two factors. The correlation declined somewhat during the 1990s but has increased again recently, standing currently at around 0.7.

For the model with two interrelated area-specific factors the results are reported in Table 5.4. As suggested by the Akaike criterion, the UK has been placed in the Continental-European area¹⁸. The North-American factor is considerably more persistent than the European one, as reflected in the high autoregressive coefficient $d_{1,1}$. Again, the North American is largely unaffected by developments in Europe, with the coefficient $d_{1,2}$ being small and insignificant and the share of Canadian and US industrial production growth variance explained by innovations in the Continental-European factor being close to zero (see Table 5.5). In contrast, the share of growth variance for the European countries explained by innovations in the North-American factor is substantially larger, especially if seen relative to the contribution of the "own" factor innovations.

¹⁷The dataset used in the estimation of the common factor in industrial production monthly rates of change spans the period 1970.M2 to 2000.M2

¹⁸The log-likelihoods for this specification is -2853.69 , compared to -2855.33 for the case where the UK is included in the North-American area.

Table 5.4 Parameter estimates (Industrial production: Model with two interrelated area-specific factors)

	U.S.A.	Canada	U.K.	Germany	France	Italy	
a_i^j	0.051 (0.077)	-0.293 (0.055)	-0.209 (0.051)	-0.442 (0.047)	-0.431 (0.048)	-0.442 (0.050)	
c_i^j	0.432 (0.079)	0.354 (0.058)	0.271 (0.064)	0.251 (0.058)	0.356 (0.063)	0.439 (0.071)	
σ_i^j	0.728 (0.054)	0.851 (0.040)	0.934 (0.038)	0.856 (0.035)	0.830 (0.040)	0.770 (0.048)	
$d_{1,1}$	0.724 (0.090)	$d_{1,2}$	0.082 (0.130)	$d_{2,1}$	0.345 (0.101)	$d_{2,2}$	0.100 (0.147)

$$Y_{i,t}^j = a_i^j Y_{i,t-1}^j + c_i^j N_{i,t} + \varepsilon_{i,t}^j \quad \forall i \quad \forall j$$

$$N_t = (d_{i,j}) N_{t-1} + \eta_t \quad i \in \{1, 2\}, j \in \{1, 2\}$$

Table 5.5 Shares of variance accounted for by the innovations of the common factors

	USA	Canada	UK	Germany	France	Italy
S_1	0.461	0.201	0.017	0.012	0.023	0.036
S_2	0.003	0.001	0.074	0.073	0.143	0.224

S_i : share of variance accounted for by the innovations of area-specific factor N_i

5.2 Sub-sample analysis

It seems reasonable to assume that the process of globalisation strengthens the cross-country linkages through which developments in one country/area spillover to other countries/areas. As past decades have been characterised by a substantial reduction of trade barriers, innovations in transportation and communication technologies and increasing financial integration, the size of spill-over effects between countries for a given shock should therefore have increased over the sample period.¹⁹ In order to analyse the evolution of spill-over effects over time we use again the GDP series and split the overall sample period into two distinct sub-periods: 1970.2-1986.1 and 1986.2-2002.2. For the second sub-period, the model specification with the UK included in the North-American area yields negative spill-overs from the Continental-European factor to the North-American factor, which are difficult to interpret economically, especially given the sign reversal between the first and second sub-period. Therefore we base our analysis on the results for the alternative specification with the UK being included in the Continental-European area.

The estimation results for the two subsamples are shown in Tables 5.6 to 5.9.

¹⁹This does not necessarily mean that the co-movement between activity in different countries/areas necessarily has increased. Apart from the possibility of increased idiosyncratic shocks, discussed earlier in the text, globalisation can also be expected to lead to increased regional specialisation, thus reducing the prevalence of common shocks across countries/area.

Table 5.6 Parameter estimates (Model with two interrelated area-specific factors)
1972.2-1986.1, UK included in the Continental-European factor

	U.S.A.	Canada	U.K.	Germany	France	Italy	
a_i^j	-0.333 (0.185)	0.150 (0.111)	-0.206 (0.117)	-0.465 (0.113)	0.097 (0.112)	0.428 (0.099)	
c_i^j	0.939 (0.160)	0.451 (0.126)	0.420 (0.155)	0.708 (0.160)	0.496 (0.140)	0.340 (0.081)	
σ_i^j	0.007 (0.702)	0.795 (0.081)	0.862 (0.083)	0.532 (0.121)	0.748 (0.080)	0.716 (0.069)	
$d_{1,1}$	0.458 (0.160)	$d_{1,2}$	0.172 (0.126)	$d_{2,1}$	0.398 (0.155)	$d_{2,2}$	0.350 (0.159)

$$Y_{i,t}^j = a_i^j Y_{i,t-1}^j + c_i^j N_{i,t} + \varepsilon_{i,t}^j \quad \forall i \quad \forall j$$

$$N_t = (d_{i,j}) N_{t-1} + \eta_t \quad i \in \{1, 2\}, j \in \{1, 2\}$$

Table 5.7 Shares of variance accounted for by the innovations of the common factors
1972.2-1986.1, UK included in the Continental-European factor

	USA	Canada	UK	Germany	France	Italy
S_1	0.961	0.330	0.047	0.107	0.102	0.098
S_2	0.039	0.017	0.185	0.535	0.323	0.250

S_i : share of variance accounted for by the innovations of area-specific factor N_i

Table 5.8 Parameter estimates (Model with two interrelated area-specific factors)
1986.2-2002.2, UK included in the Continental-European factor

	U.S.A.	Canada	U.K.	Germany	France	Italy	
a_i^j	-0.064 (0.115)	-0.228 (0.185)	0.494 (0.113)	-0.062 (0.119)	-0.096 (0.144)	-0.355 (0.117)	
c_i^j	0.471 (0.139)	0.758 (0.119)	0.136 (0.143)	0.243 (0.135)	0.587 (0.079)	0.534 (0.253)	
σ_i^j	0.771 (0.079)	0.319 (0.253)	0.792 (0.071)	0.931 (0.085)	0.531 (0.116)	0.698 (0.091)	
$d_{1,1}$	0.723 (0.138)	$d_{1,2}$	-0.056 (0.120)	$d_{2,1}$	0.447 (0.143)	$d_{2,2}$	0.475 (0.139)

$$Y_{i,t}^j = a_i^j Y_{i,t-1}^j + c_i^j N_{i,t} + \varepsilon_{i,t}^j \quad \forall i \quad \forall j$$

$$N_t = (d_{i,j}) N_{t-1} + \eta_t \quad i \in \{1, 2\}, j \in \{1, 2\}$$

Table 5.9 Shares of variance accounted for by the innovations of the common factors
1986.2-2002.2, UK included in the Continental-European factor

	USA	Canada	UK	Germany	France	Italy
S_1	0.399	0.883	0.062	0.053	0.297	0.163
S_2	0.003	0.006	0.051	0.071	0.413	0.291

S_i : share of variance accounted for by the innovations of area-specific factor N_i

Overall, it appears that the structure of the dynamic relationships between G7 growth developments has changed noticeably over time, as suggested by the dif-

ferences in the estimated parameters between the two sub-periods. In particular, the dynamics of the common factors appear to have changed. The persistence of both, the North-American and the Continental-European factor has increased over time, especially in the case of the former. As to spill-over effects, the size of the $d_{1,2}$ coefficient, measuring the effect of the Continental-European factor on the North-American factor, declined between the first and second sub-period, turning slightly negative in the latter. However, in both sub-periods the coefficient is insignificant. In contrast, the coefficient $d_{2,1}$ is significant and positive in both sub-periods. Furthermore the coefficient increased over time. These findings thus suggest that Europe may have become more susceptible to shocks originating in North-America, while North America remains insulated from developments in Europe.

Regarding the shares of variance explained by innovations in the two common factors, the share attributable to the North-American factor has increased over time for most countries, with the increase for Canada, France and Italy being particularly pronounced. In contrast, in the case of the US and Germany the share has declined. The share of variance explained by the Continental-European factor has declined for most countries, with the exception of France and Italy. Among the European countries the shares for the UK and Germany declined significantly, which in the latter case might partly be explained by idiosyncratic movements associated with the economic ramifications of re-unification. The changes over time are also illustrated by the impulse response function for the respective sub-periods. A shock to the North-American-specific factor has clearly stronger repercussions on the Italian and French growth rates in the second period than in the first one. Moreover, with the exception of Italy, we can observe that the responses are more persistent during the second period.

(Insert Figure 13 and 14 here)

6 Conclusion

The paper identifies a number of stylised facts about the observed common fluctuations among G7 real GDP growth rates and tries to disentangle the contribution of common shocks - in particular, oil price fluctuations - and cross-country/cross-area spill-over effects in determining those joint fluctuations.

The estimation of a dynamic common factor model for the G7 countries' GDP (and industrial production) growth using Kalman filtering techniques allows first to isolate and measure the historical evolution of the degree of output growth comovements in the different countries. The general model specification assumes the process for real GDP growth in each of the G7 countries to be driven by a country-specific autoregressive component and a latent component, which is common to all series and follows a univariate autoregressive process.

By extending the model so to include "area-wide" common factors which are each shared by only a subset of countries, the paper also disentangles "area-wide" common factors and "area-wide" spill-over effects.

An important result of the analysis is to show that the G7 countries share common output dynamics with clearly identifiable common swings in activity across the G7. Furthermore, the paper finds statistical support for a (time-varying) effect of oil price developments on the common factor, confirming that oil prices, indeed, constitute one important variable partly responsible for the observed co-movement among economic activity in different countries. Furthermore, the evolution of idiosyncratic and common shocks is consistent with the possible increase of the relevance of spillover effects in driving the shared dynamics of real GDP developments.

The "area-wide" specification of common factors identifies significant "area-wide" common effects on real GDP growth developments in the G7 countries and strong spill-over effects running from the North-American area to the European area, but not vice versa. Similar results are obtained when a factor common to the G7 industrial production series is estimated.

The paper provides a number of interesting insights for future research. In particular, one line of investigation would be to deepen the understanding of the economic determinants of common fluctuations and area linkages, especially looking at the developments in the last two decades. In that respect, the asymmetry between North America and (Continental) Europe as a source of spill-over effects would be worth exploring further. For that purpose a more careful analysis of the characteristics of the channels of international transmission of country-specific shocks would be useful.

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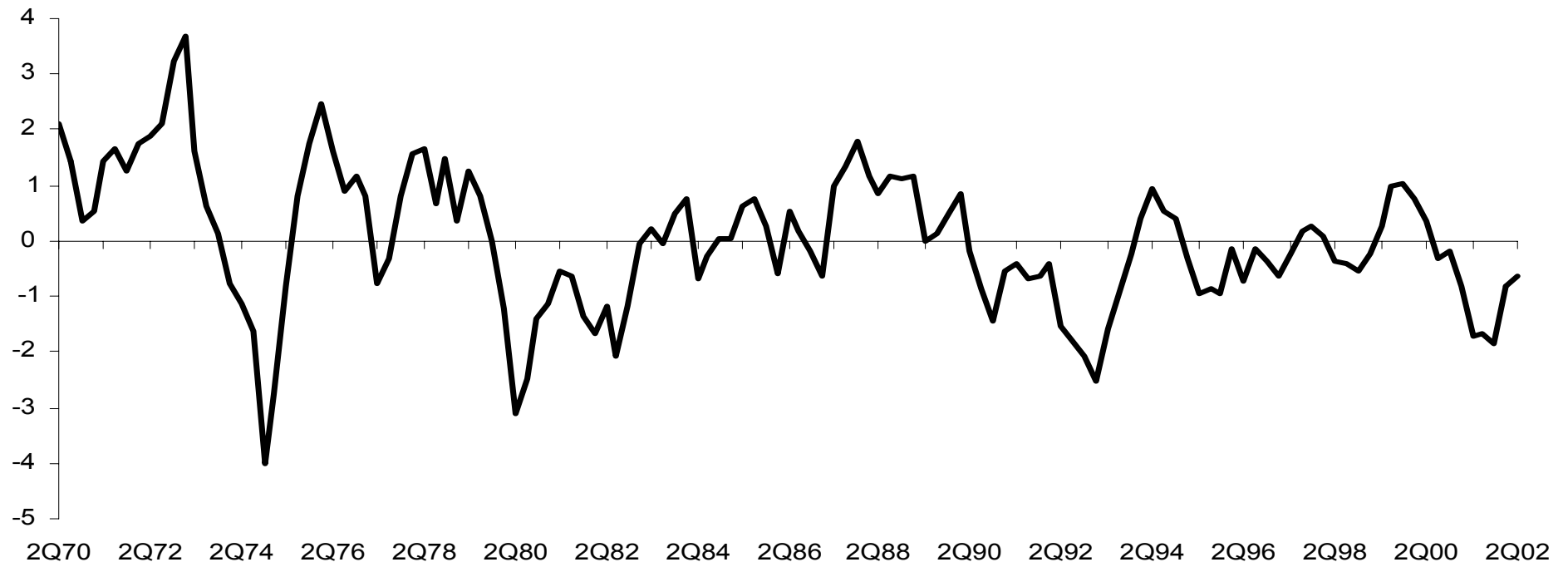
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Figure 1

G7 common factor in real GDP growth

(QoQ, % change)

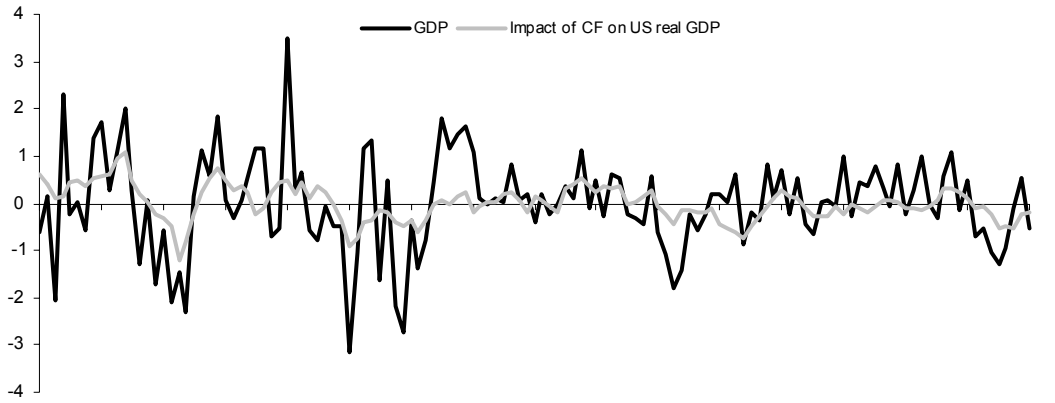


1 common factor and no spillovers

Figure 2

US - Real GDP growth rates: actual and impact contribution of the common factor

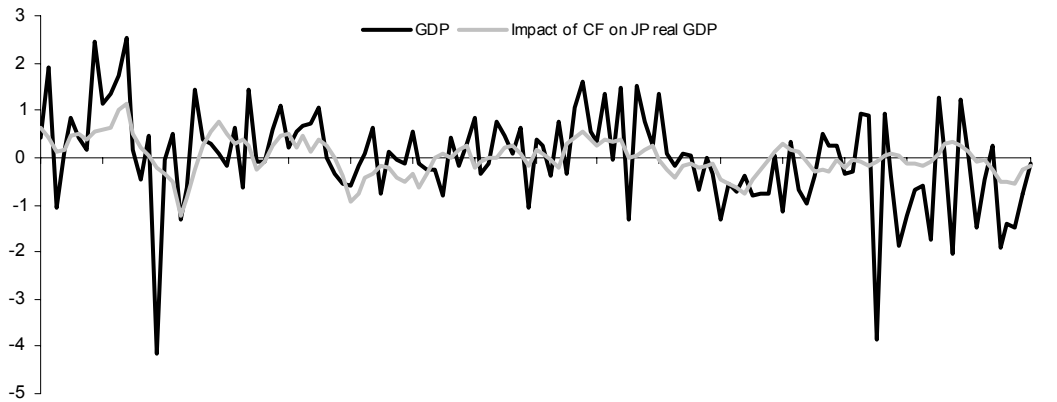
(QoQ, % change)



1 common factor and no spillovers. Real GDP series are standardised

JAP - Real GDP growth rates: actual and impact contribution of the common factor

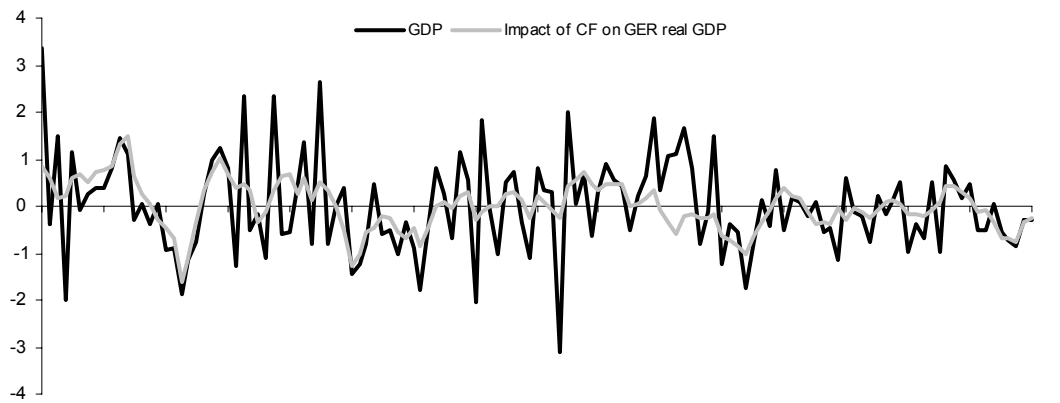
(QoQ, % change)



1 common factor and no spillovers. Real GDP series are standardised

GER - Real GDP growth rates: actual and impact contribution of the common factor

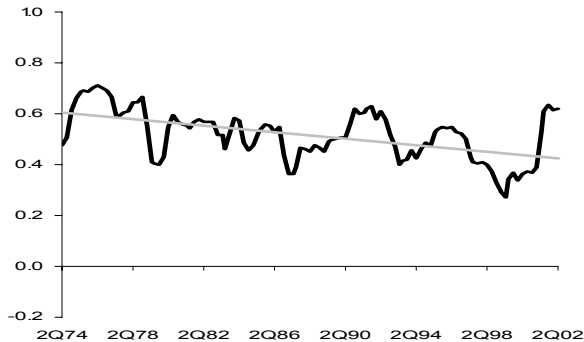
(QoQ, % change)



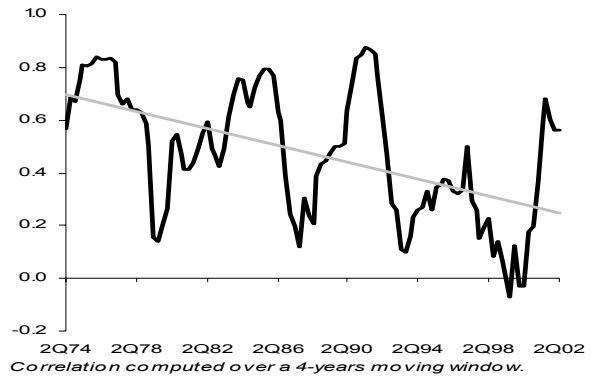
1 common factor and no spillovers. Real GDP series are standardised

Figure 3

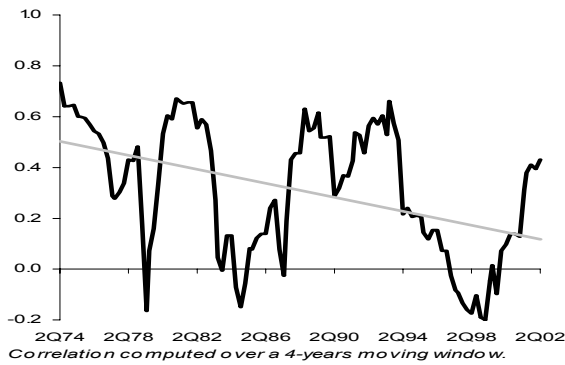
G7 - GDP growth - common factor correlation



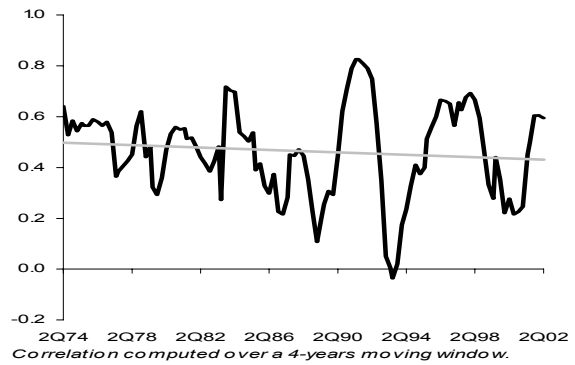
US - GDP growth - common factor correlation



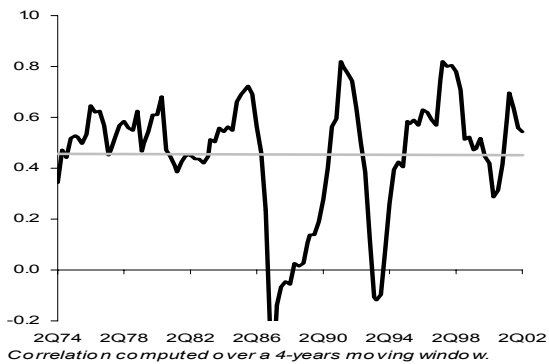
JAP - GDP growth - common factor correlation



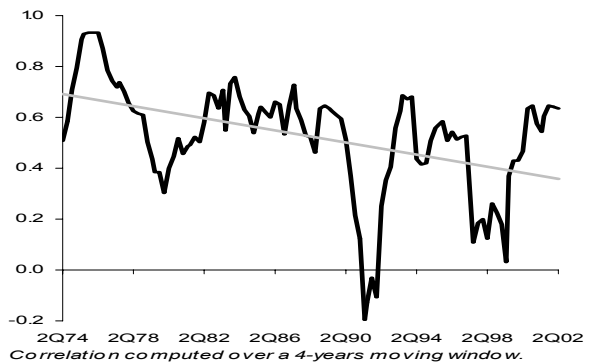
UK - GDP growth - common factor correlation



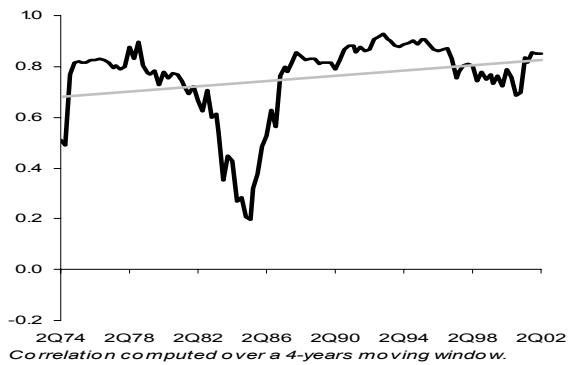
CAD - GDP growth - common factor correlation



GER - GDP growth - common factor correlation



FRA - GDP growth - common factor correlation



ITA - GDP growth - common factor correlation

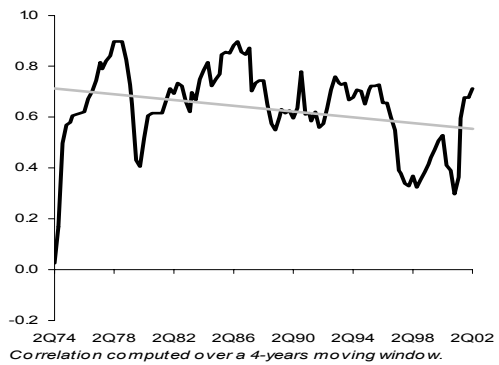
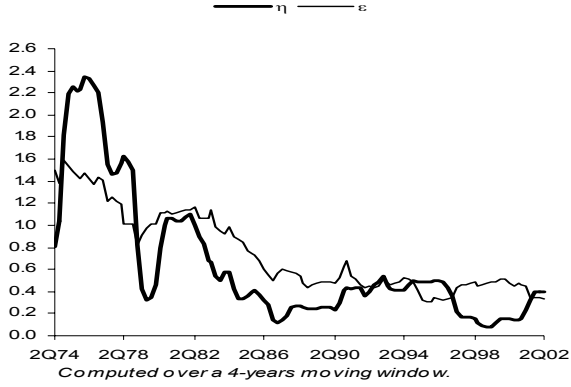
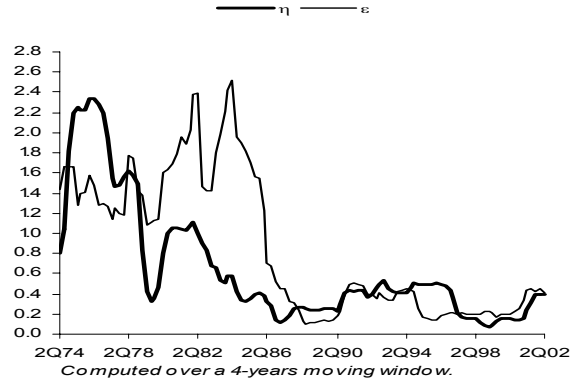


Figure 4

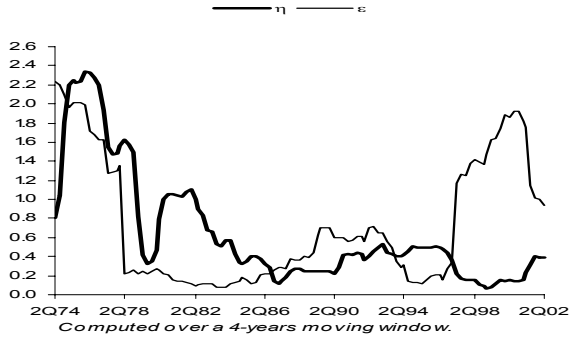
Average G7 - Variance of common and idiosyncratic shocks



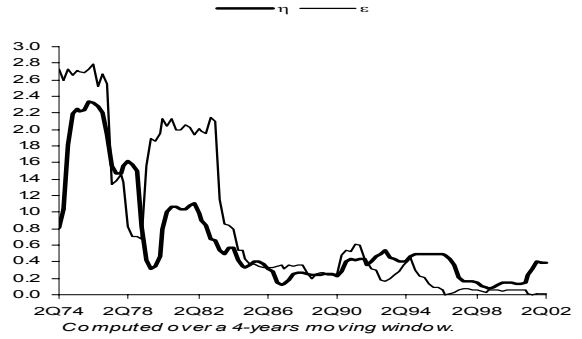
US - Variance of common and idiosyncratic shocks



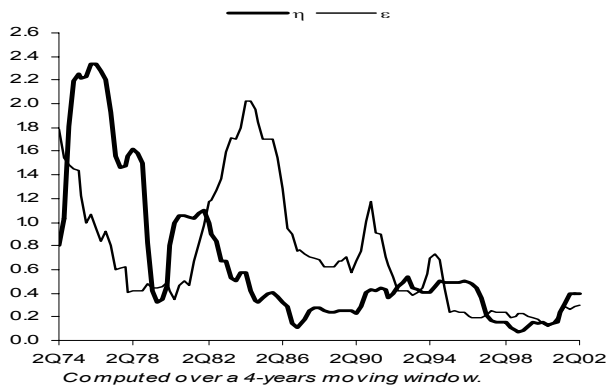
JP - Variance of common and idiosyncratic shocks



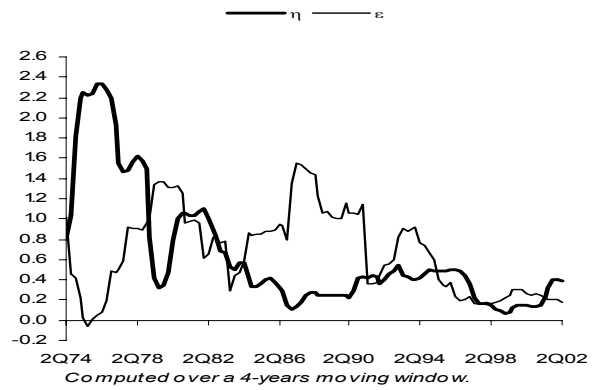
UK - Variance of common and idiosyncratic shocks



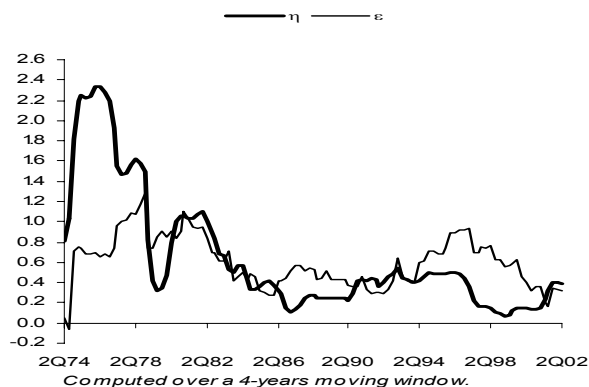
CAD - Variance of common and idiosyncratic shocks



GER - Variance of common and idiosyncratic shocks



FRA - Variance of common and idiosyncratic shocks



ITA - Variance of common and idiosyncratic shocks

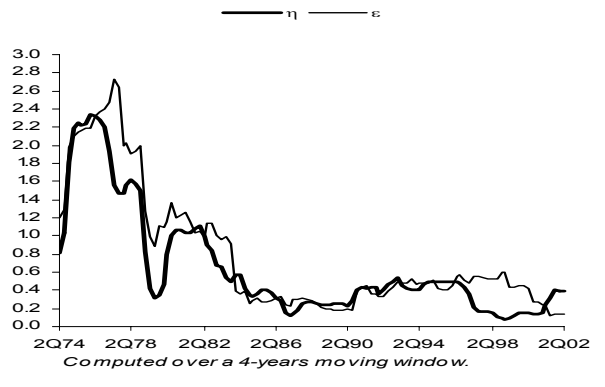


Figure 5

G7 common factor: actual and structural static forecast. Whole sample.

(structural forecast obtained from the regression of the common factor on log differences of oil prices)

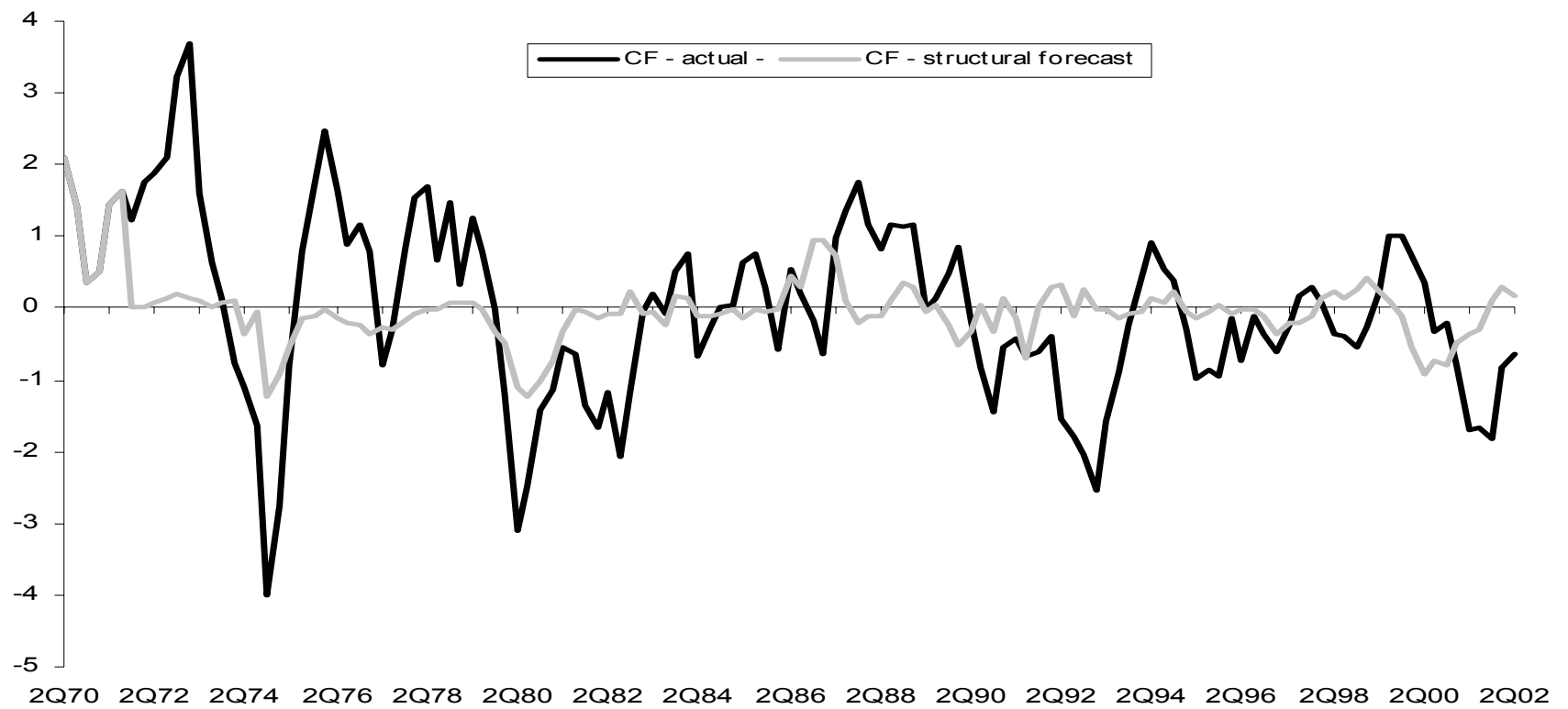


Figure 6

G7 common factor: actual and structural static forecast. Sample: 1970Q2 - 1986Q1.

(structural forecast obtained from the regression of the common factor on log differences of oil prices)

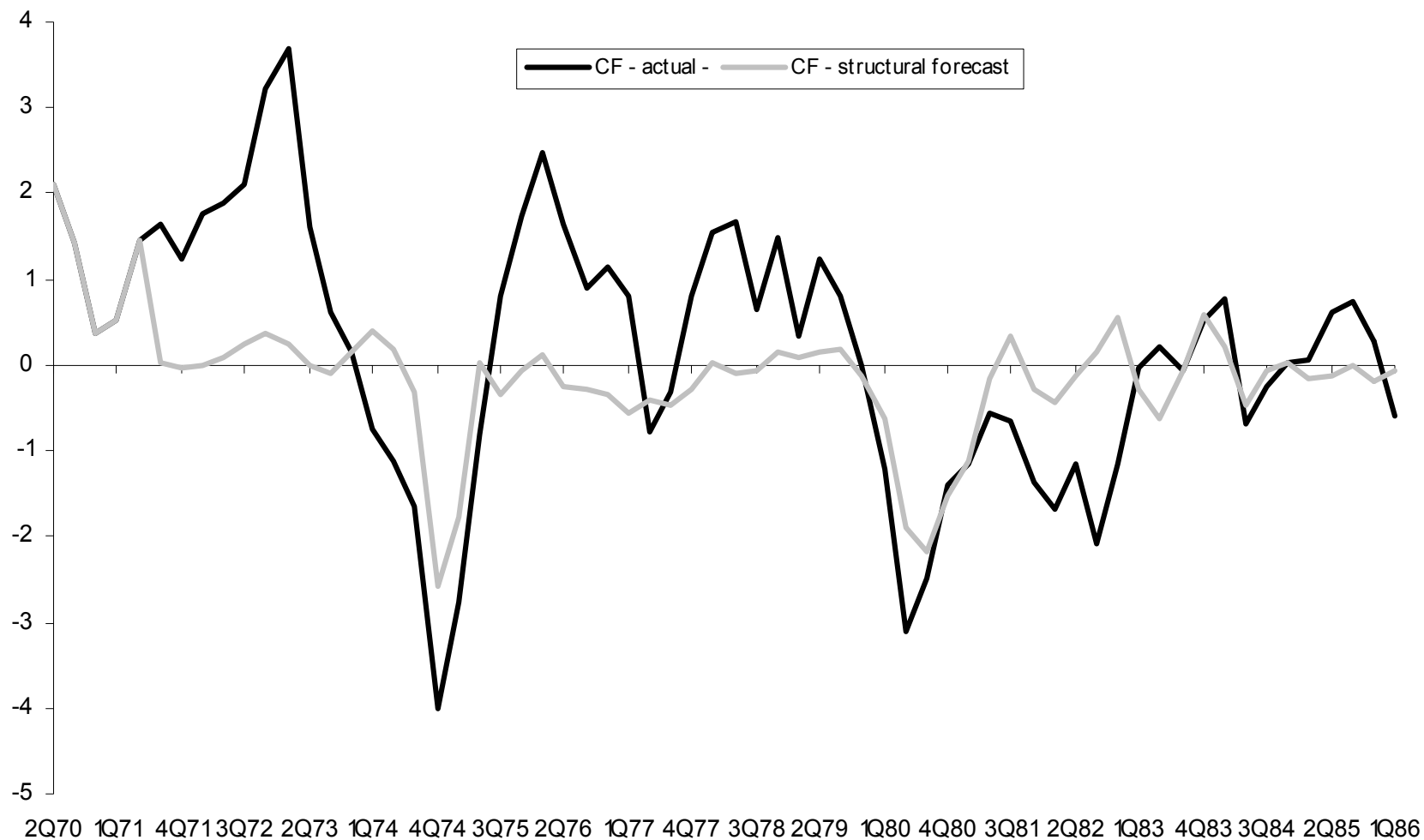


Figure 7

G7 common factor: actual and structural static forecast. Sample: 1986Q2 - 2002Q2.

(structural forecast obtained from the regression of the common factor on log differences of oil prices)

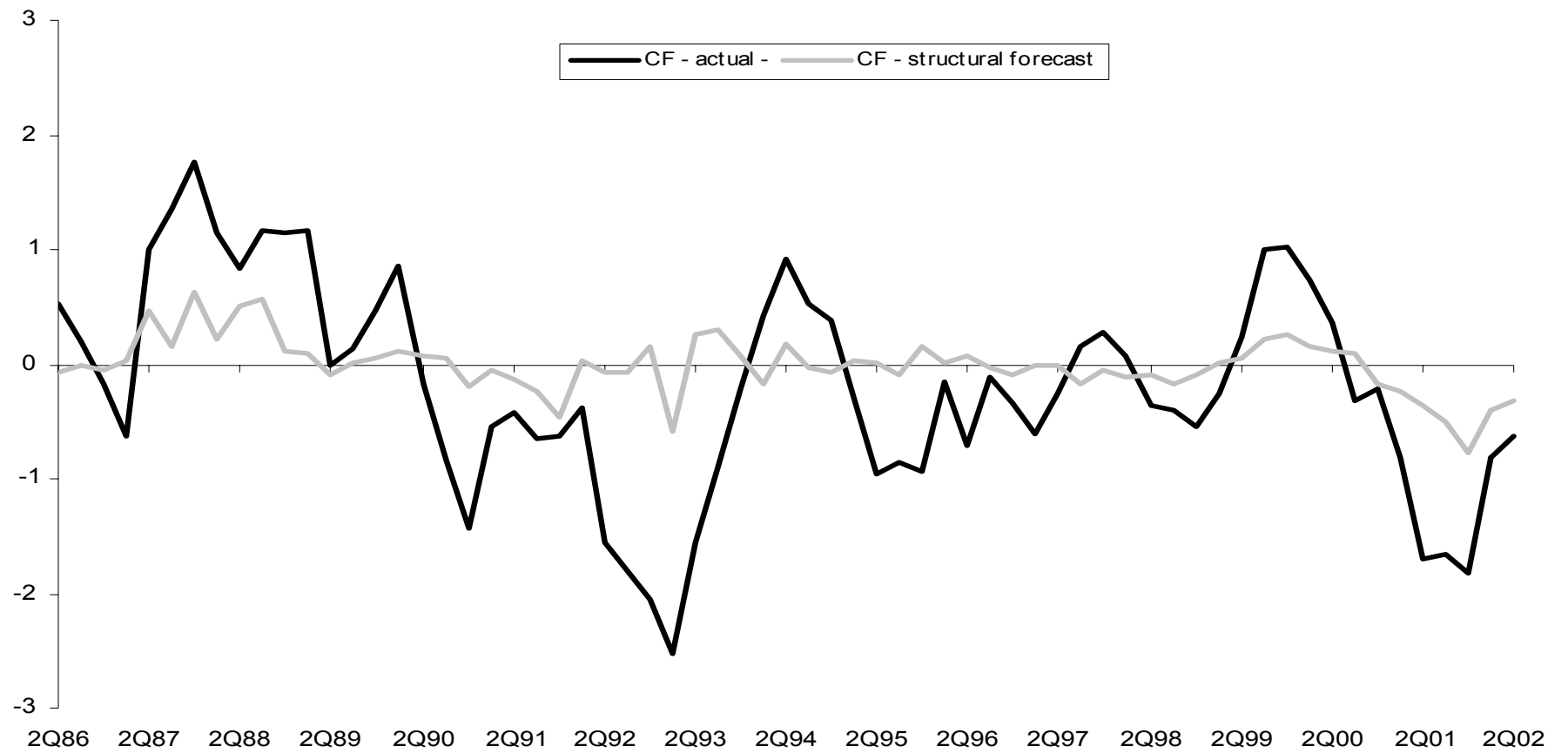
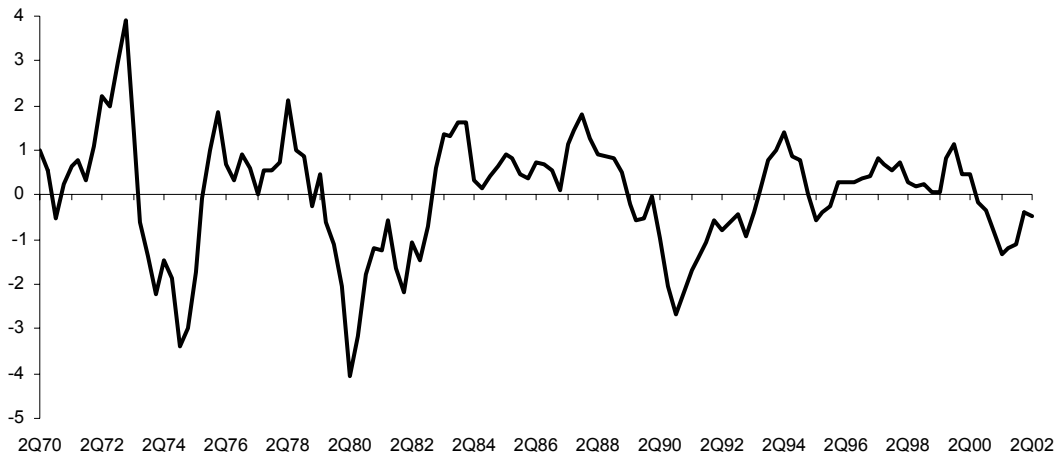


Figure 8

G7 common factor in real GDP growth

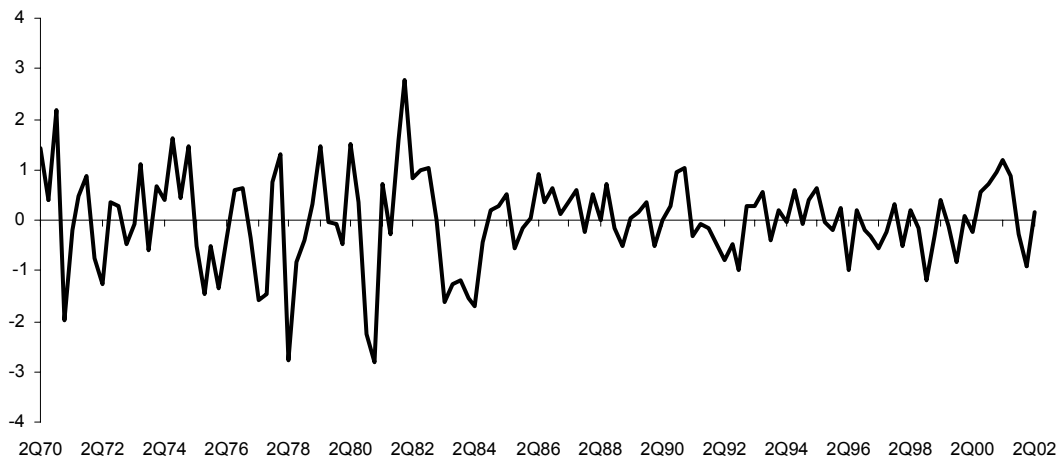
(QoQ, % change)



1 common factor, 2 regional factors and no spillovers. UK in the North-American factor

North-American factor in real GDP growth

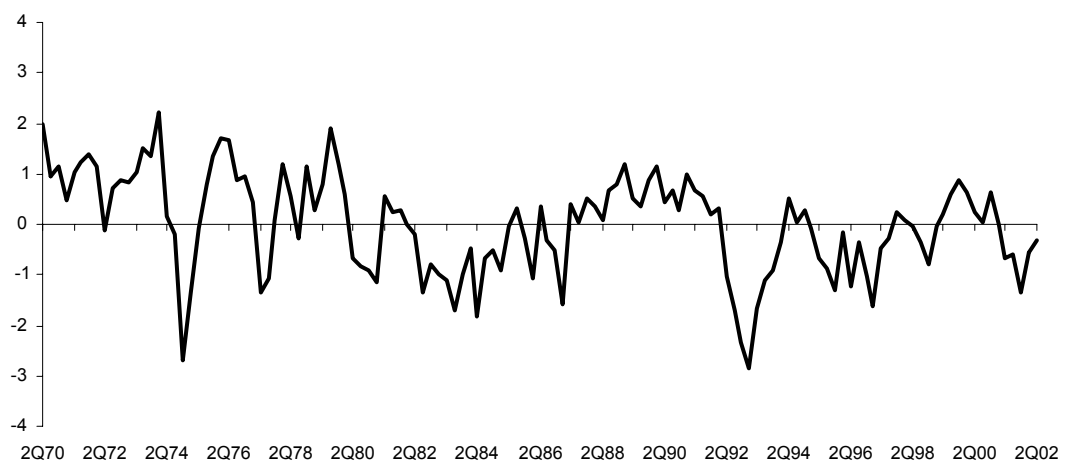
(QoQ, % change)



1 common factor, 2 regional factors and no spillovers. UK in the North-American factor

Continental European factor in real GDP growth

(QoQ, % change)

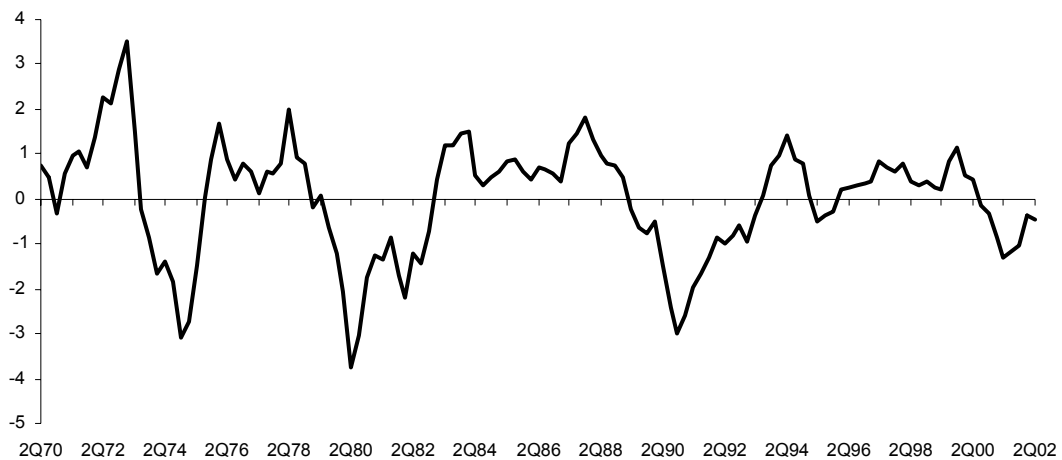


1 common factor, 2 regional factors and no spillovers. UK in the North-American factor

Figure 9

G7 common factor in real GDP growth

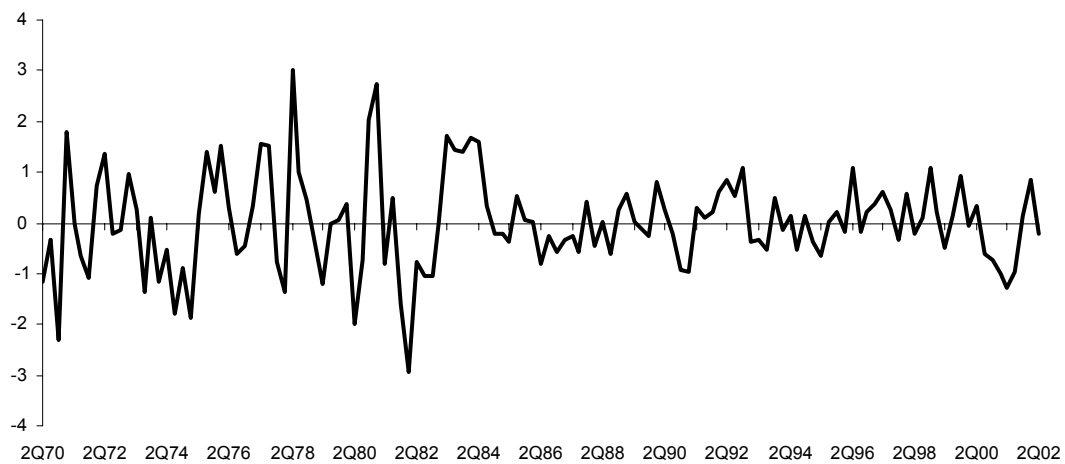
(QoQ, % change)



1 common factor, 2 regional factors and no spillovers. UK in the Continental European factor

North-American factor in real GDP growth

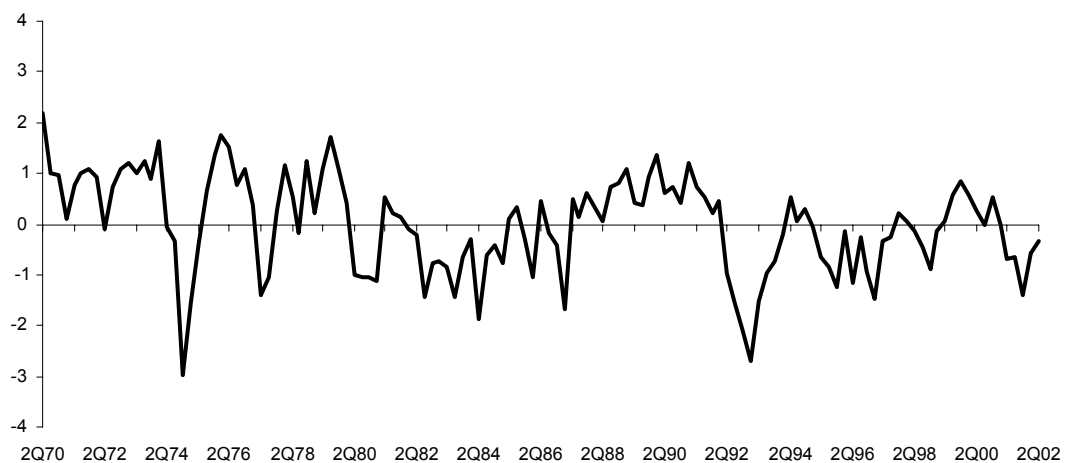
(QoQ, % change)



1 common factor, 2 regional factors and no spillovers. UK in the Continental European factor

Continental European factor in real GDP growth

(QoQ, % change)

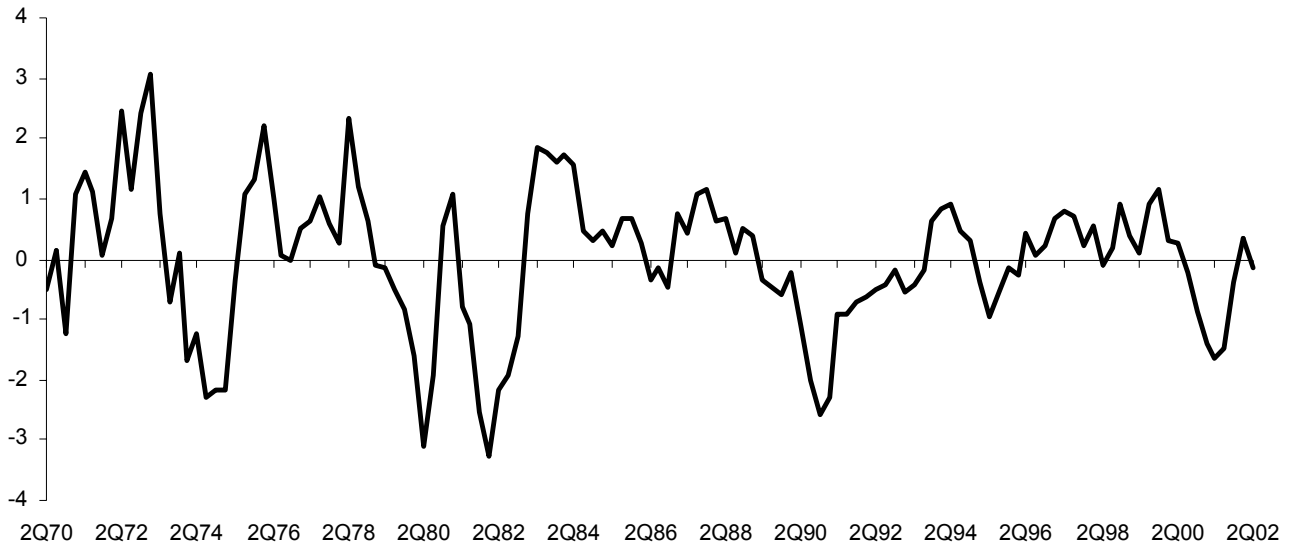


1 common factor, 2 regional factors and no spillovers. UK in the Continental European factor

Figure 10

North- American common factor

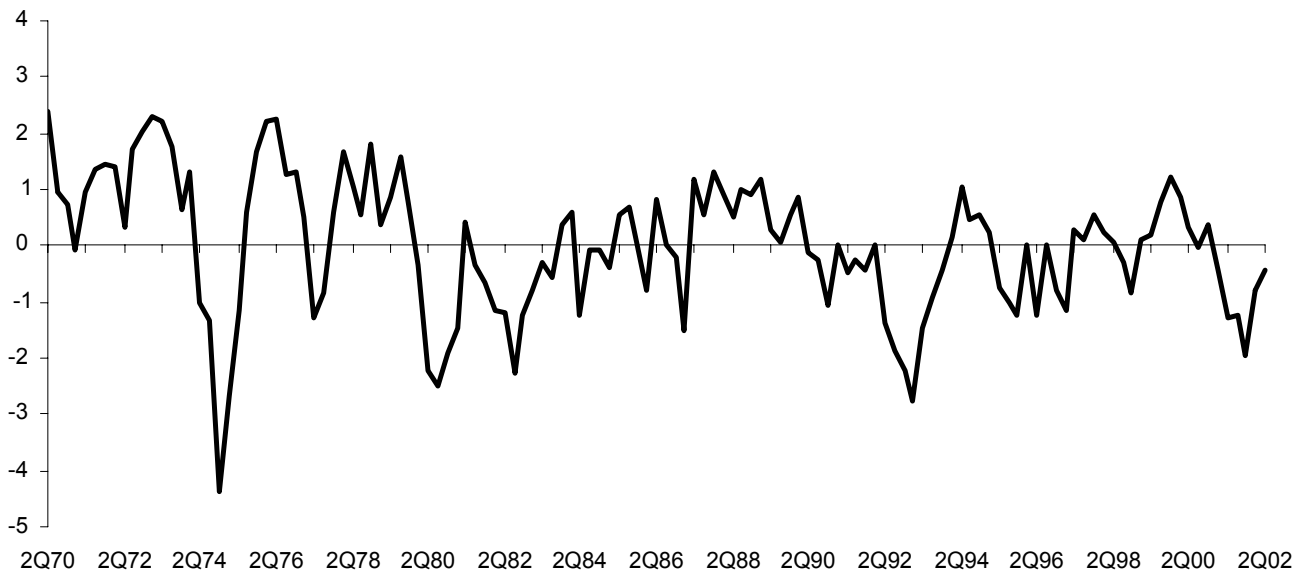
(QoQ, % change)



2 regional factors with spillovers. UK in North-American area. Whole sample

Continental European common factor

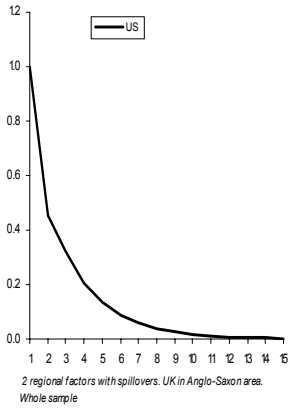
(QoQ, % change)



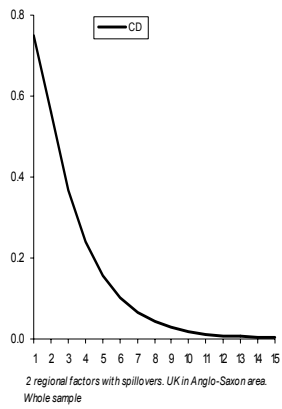
2 regional factors with spillovers. UK in North-American area. Whole sample

Figure 11

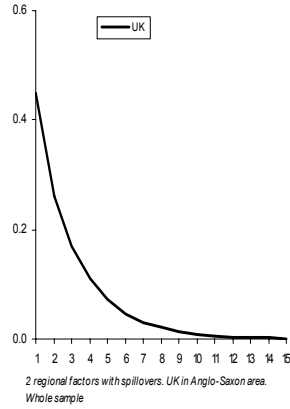
Impulse response to shock on North-American factor



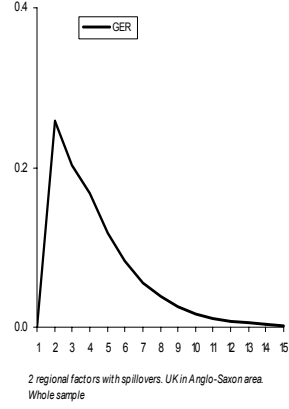
Impulse response to shock on North-American factor



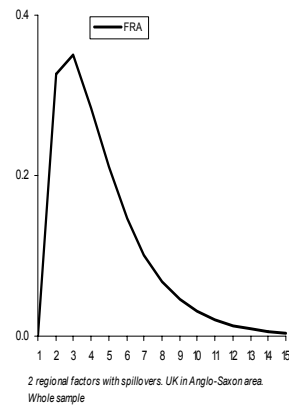
Impulse response to shock on North-American factor



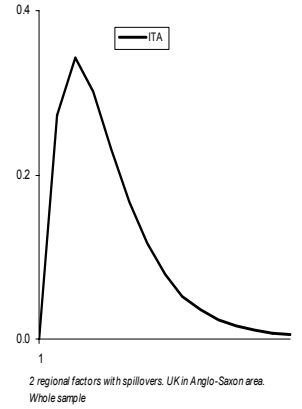
Impulse response to shock on North-American factor



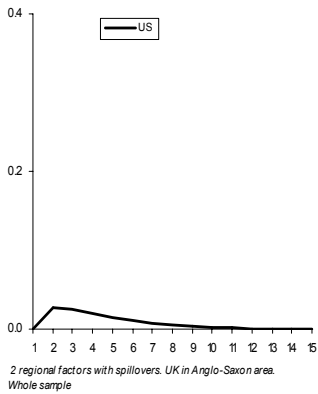
Impulse response to shock on North-American factor



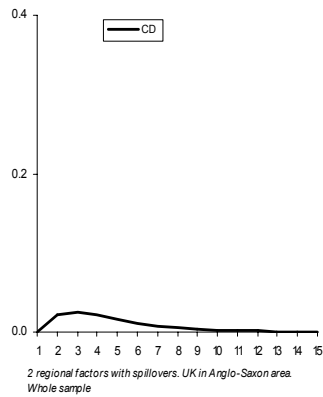
Impulse response to shock on North-American factor



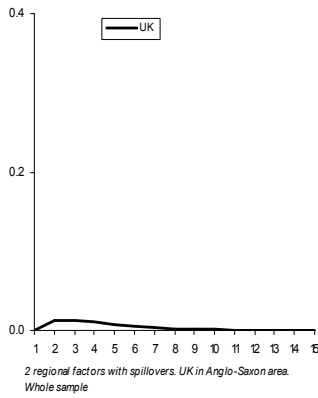
Impulse response to shock on Continental European factor



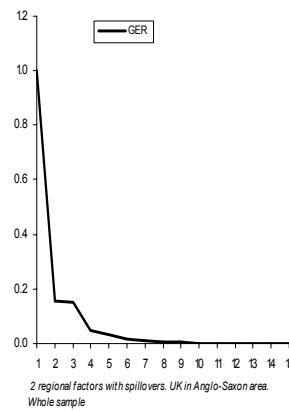
Impulse response to shock on Continental European factor



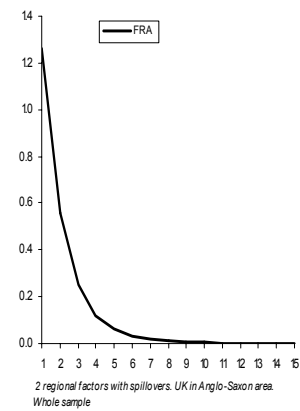
Impulse response to shock on Continental European factor



Impulse response to shock on Continental European factor



Impulse response to shock on Continental European factor



Impulse response to shock on Continental European factor

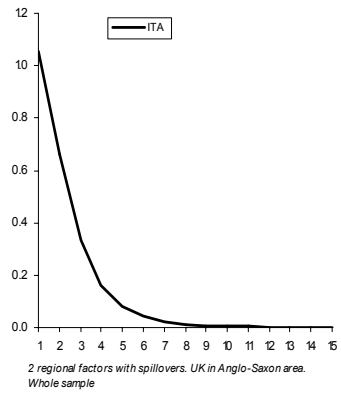
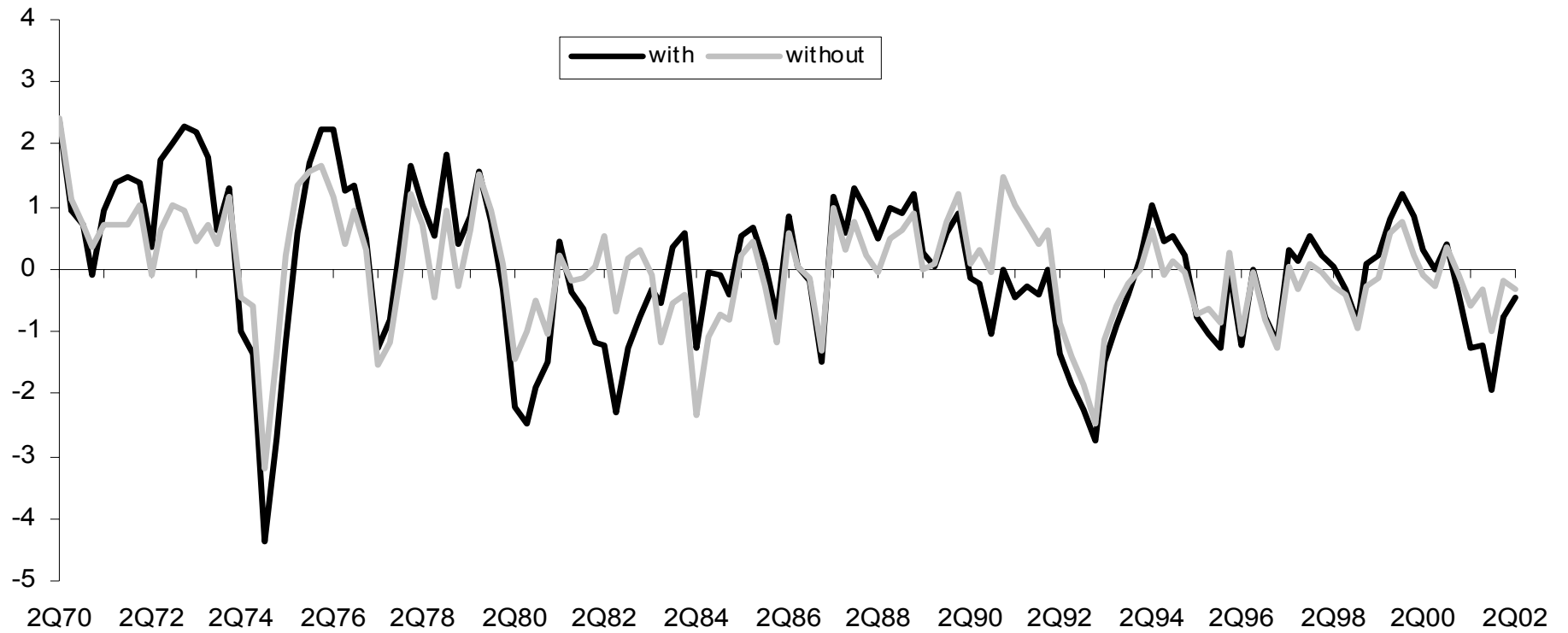


Figure 12

Continental European (with and without the contribution of North-American specific innovations)

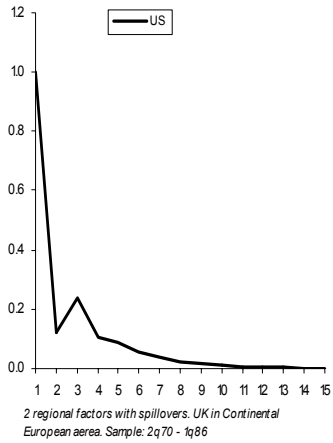
(QoQ, % change)



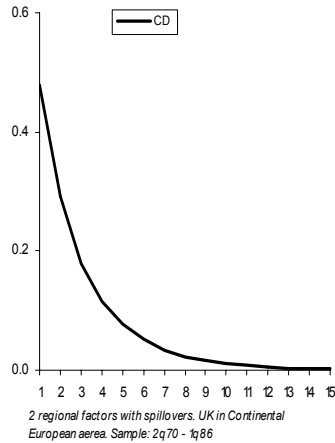
2 regional factors with spillovers. UK in North-American area. Whole sample

Figure 13

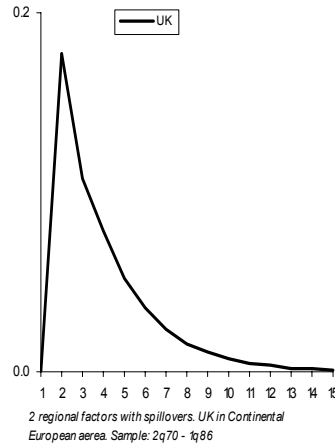
Impulse response to shock on North-American factor



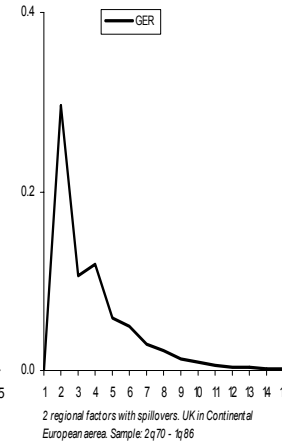
Impulse response to shock on North-American factor



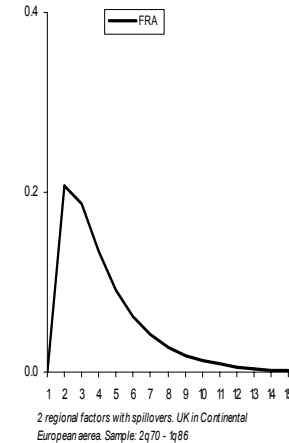
Impulse response to shock on North-American factor



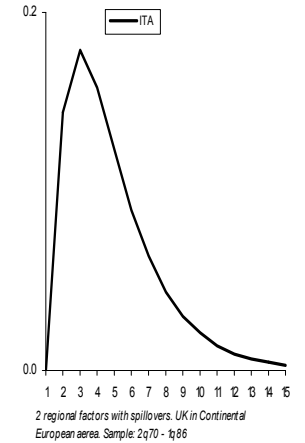
Impulse response to shock on North-American factor



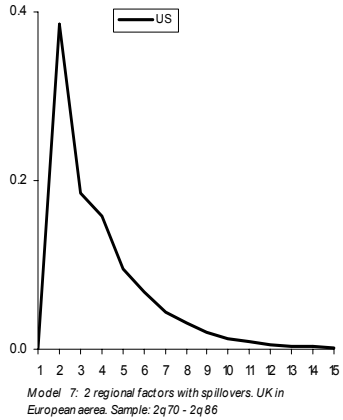
Impulse response to shock on North-American factor



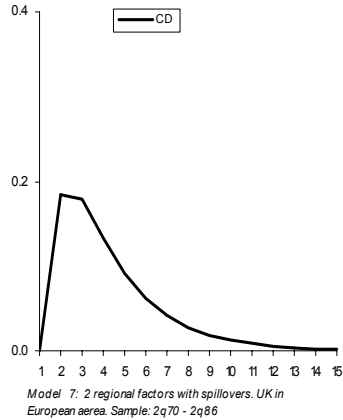
Impulse response to shock on North-American factor



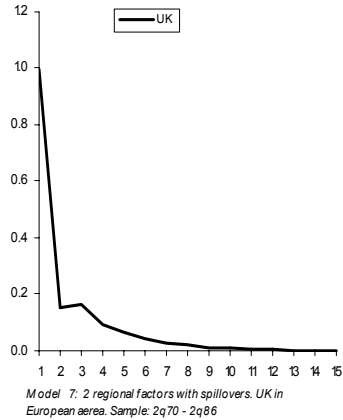
Impulse response to shock on European factor



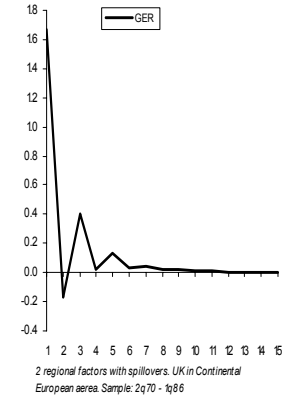
Impulse response to shock on European factor



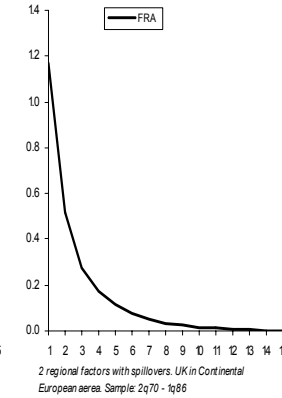
Impulse response to shock on European factor



Impulse response to shock on Continental European factor



Impulse response to shock on Continental European factor



Impulse response to shock on Continental European factor

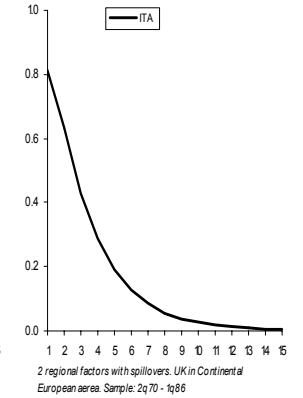


Figure 14

